

Development and Validation of Data Assimilative East Sea Regional Ocean Model

Kyung-II Chang¹, Young Ho Kim², Gyun-Do Park¹, Young-Gyu Kim³

¹Research Institute of Oceanography/School of Earth and Environmental
Sciences, Seoul National University

²Coastal Engineering Research Department, Korea Ocean Research and
Development Institute

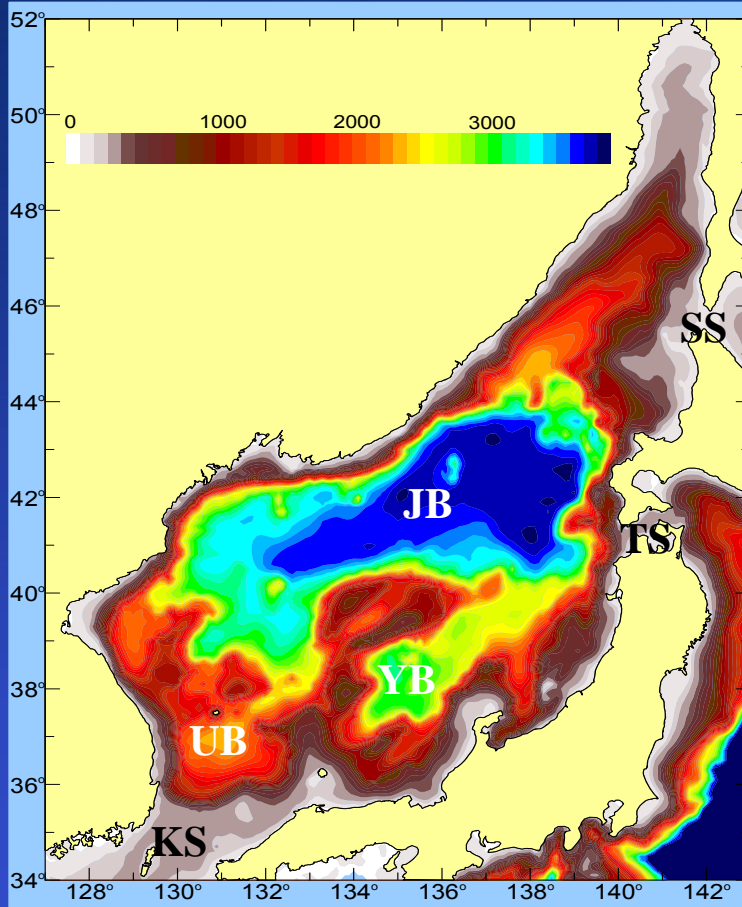
³Agency for Defense Development



Contents

- 1 East Sea & Regional Ocean Model
- 2 Implementation of 3D-Var
- 3 Validation of 3D-Var system
- 4 Future Work : Ensemble Kalman Filter
- 5 Conclusion

Regional setting: East Sea



Area: 10^6 km²

Mean depth: ~1700 m

Max. depth: ~4000 m

JB: Japan Basin

UB: Ulleung Basin

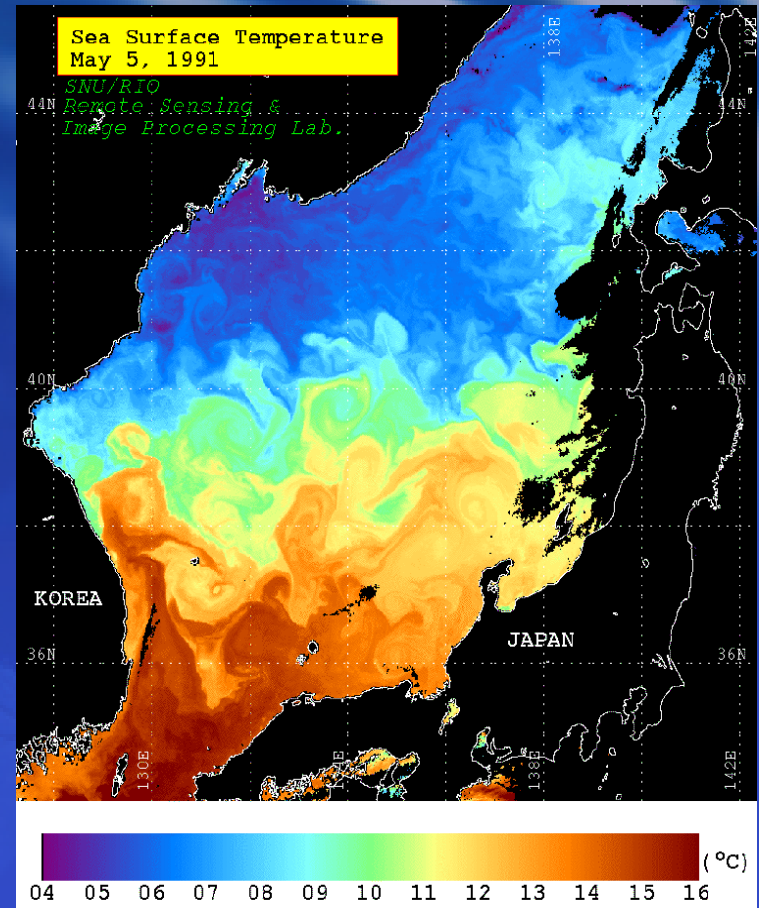
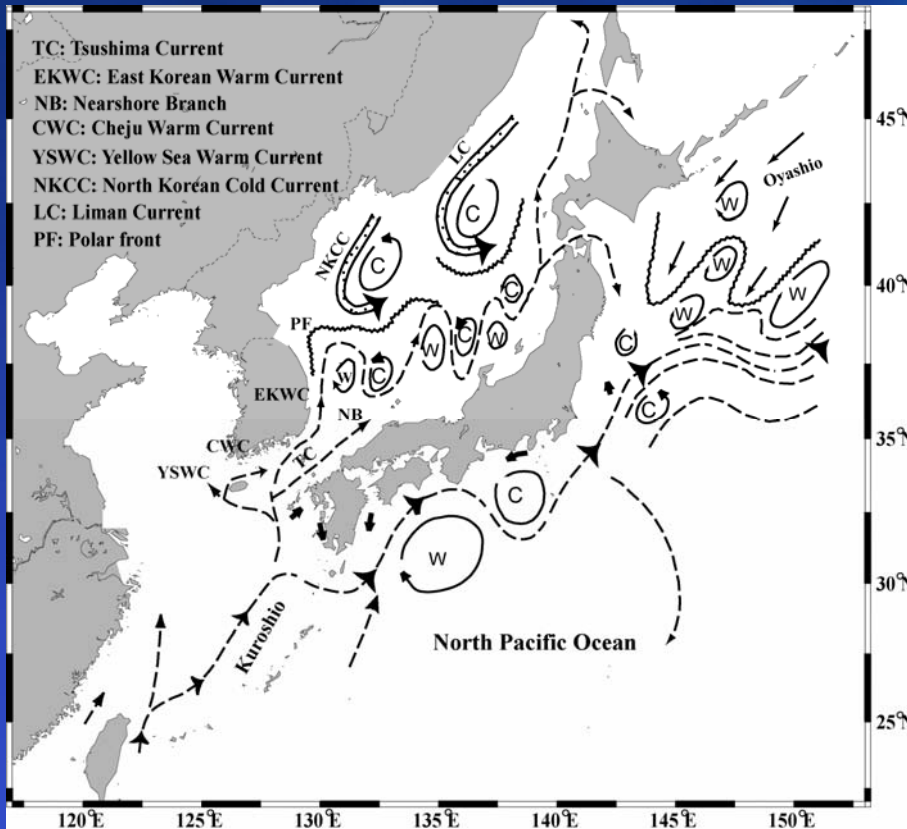
YB: Yamato Basin

KS: Korea Strait

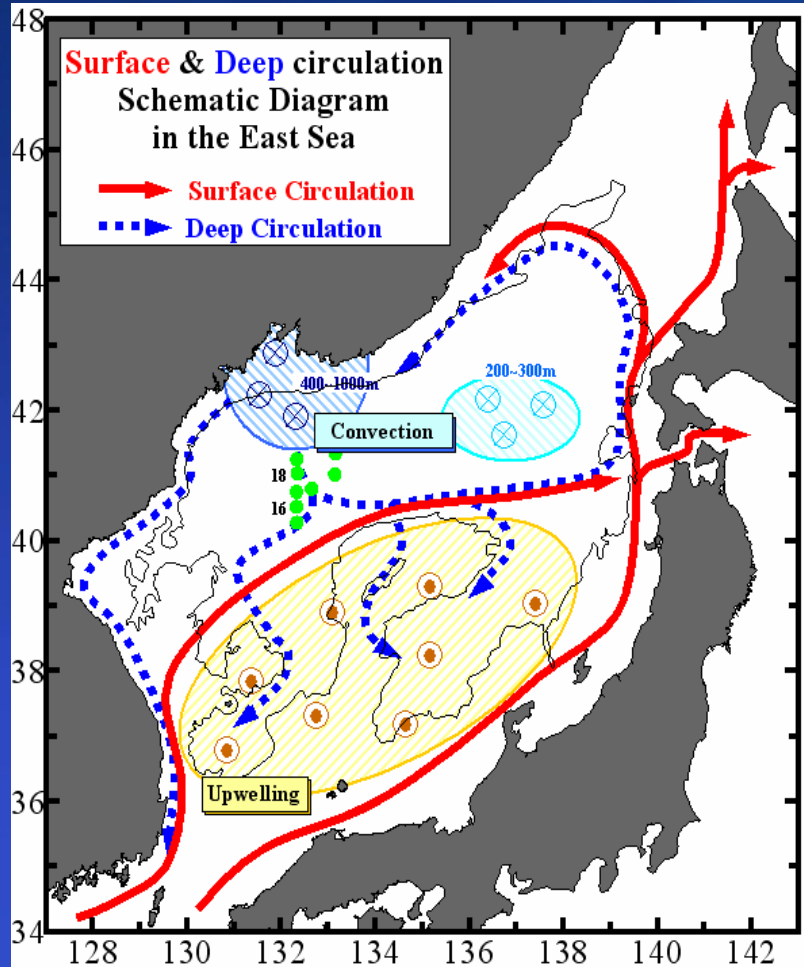
TS: Tsugaru Strait

SS: Soya Strait

Regional setting: East Sea



Regional setting: Circulation

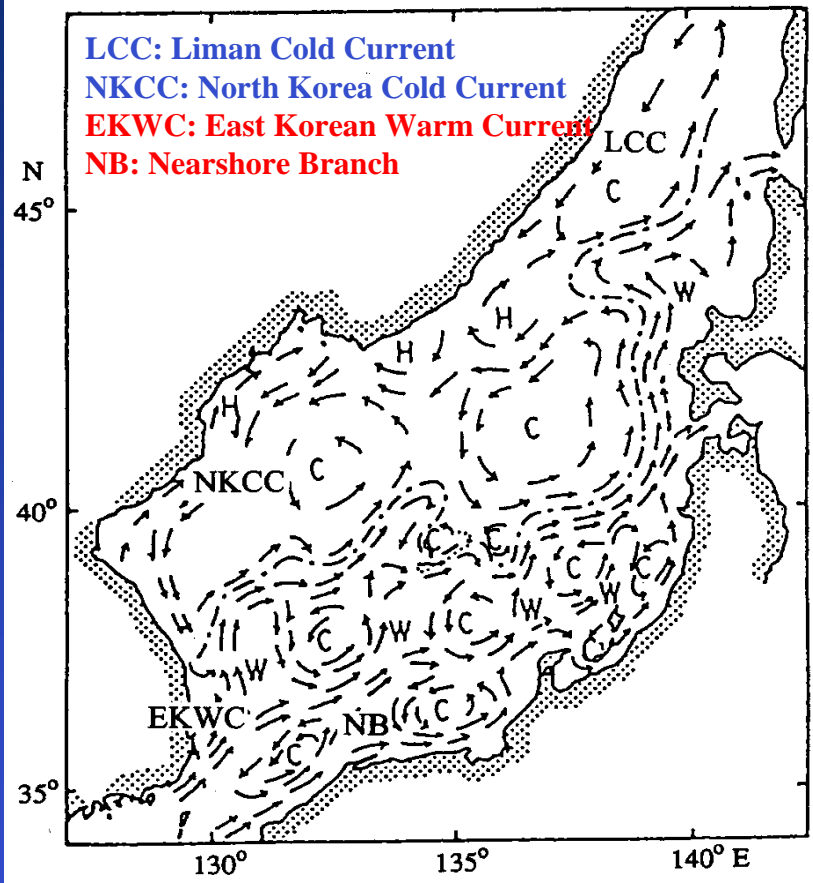


Miniature Ocean

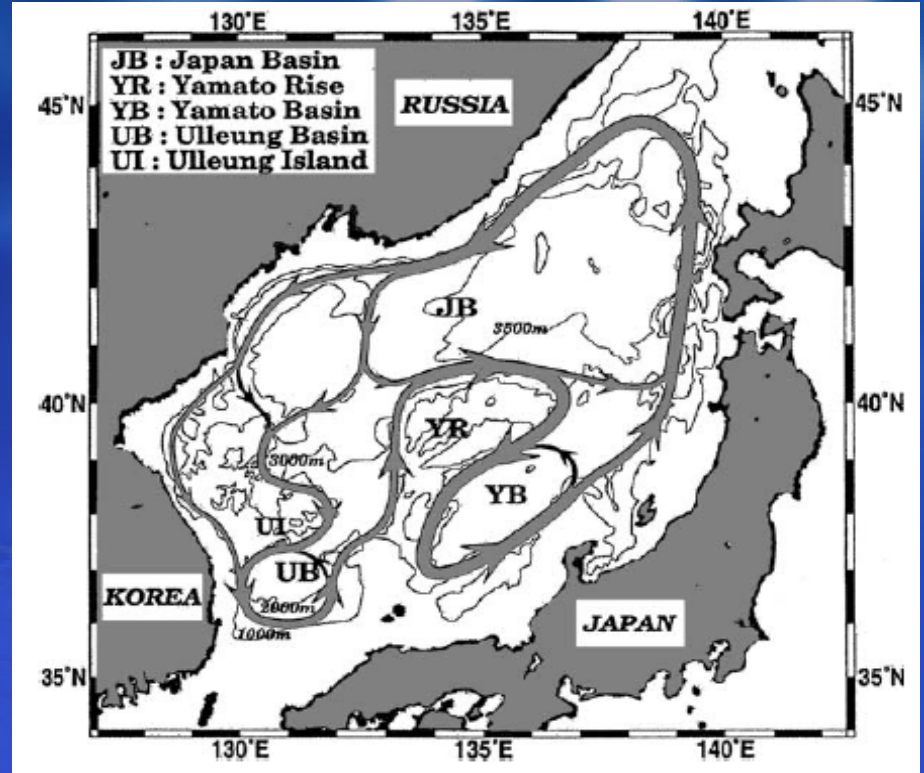
- Warm & cold water regions
- Subpolar front
- Deep water formation
- Deep circulation
- Double-gyre upper circulation
- Mesoscale eddies

Courtesy of Dr. J.J. Park

Regional setting: Circulation

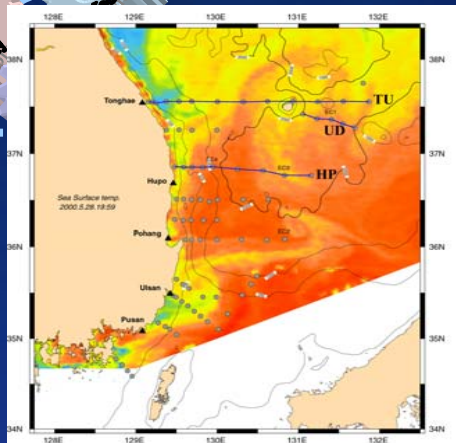


Naganuma (1977)



Senju et al. (2005)

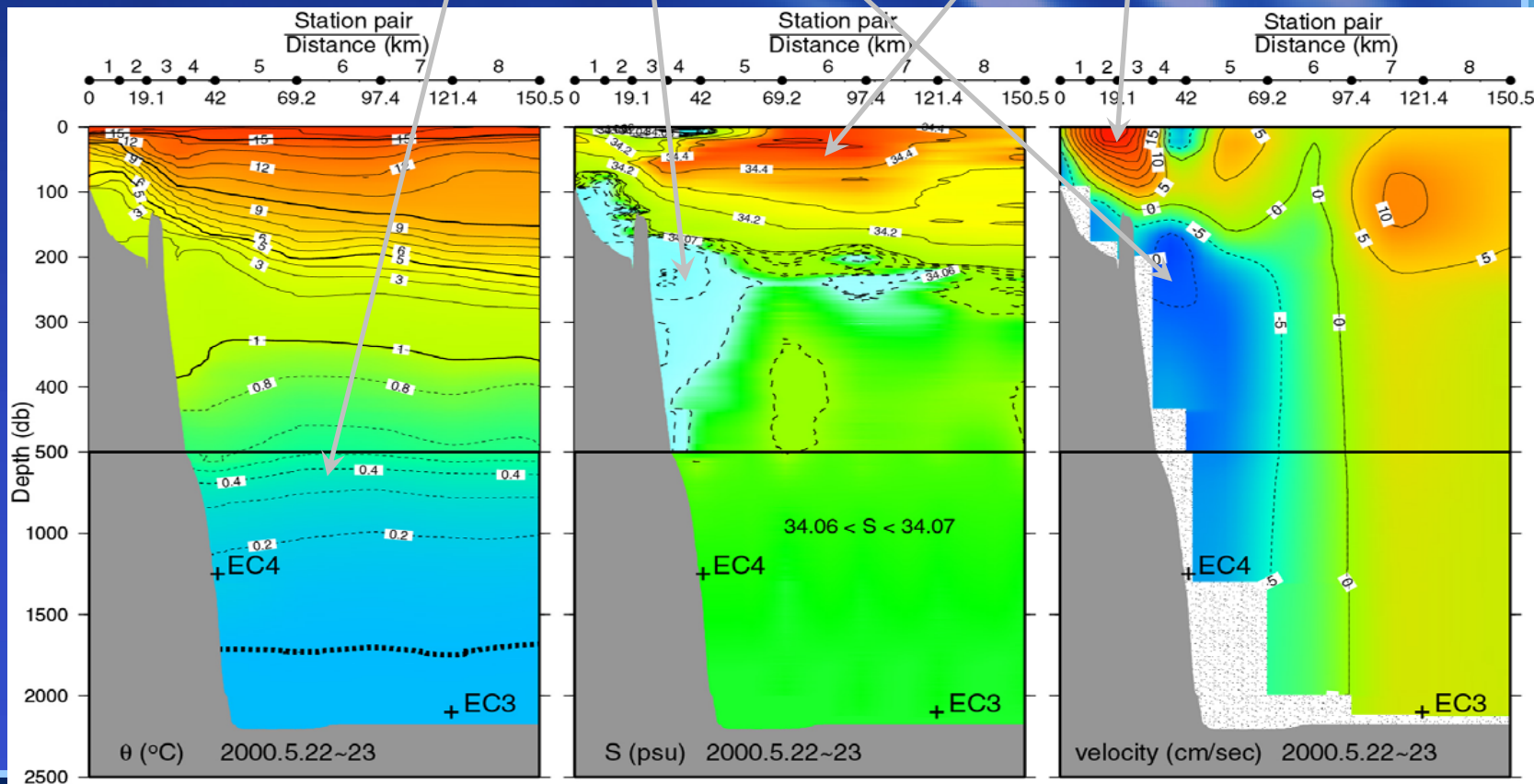
Regional setting: Water Masses



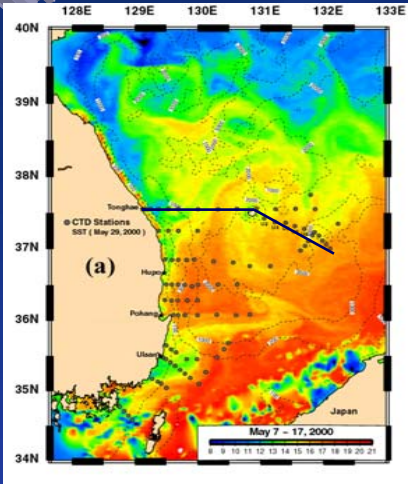
North Korean Cold Water
(Coastal mode of the East Sea Intermediate Water)

Tsushima Current Water

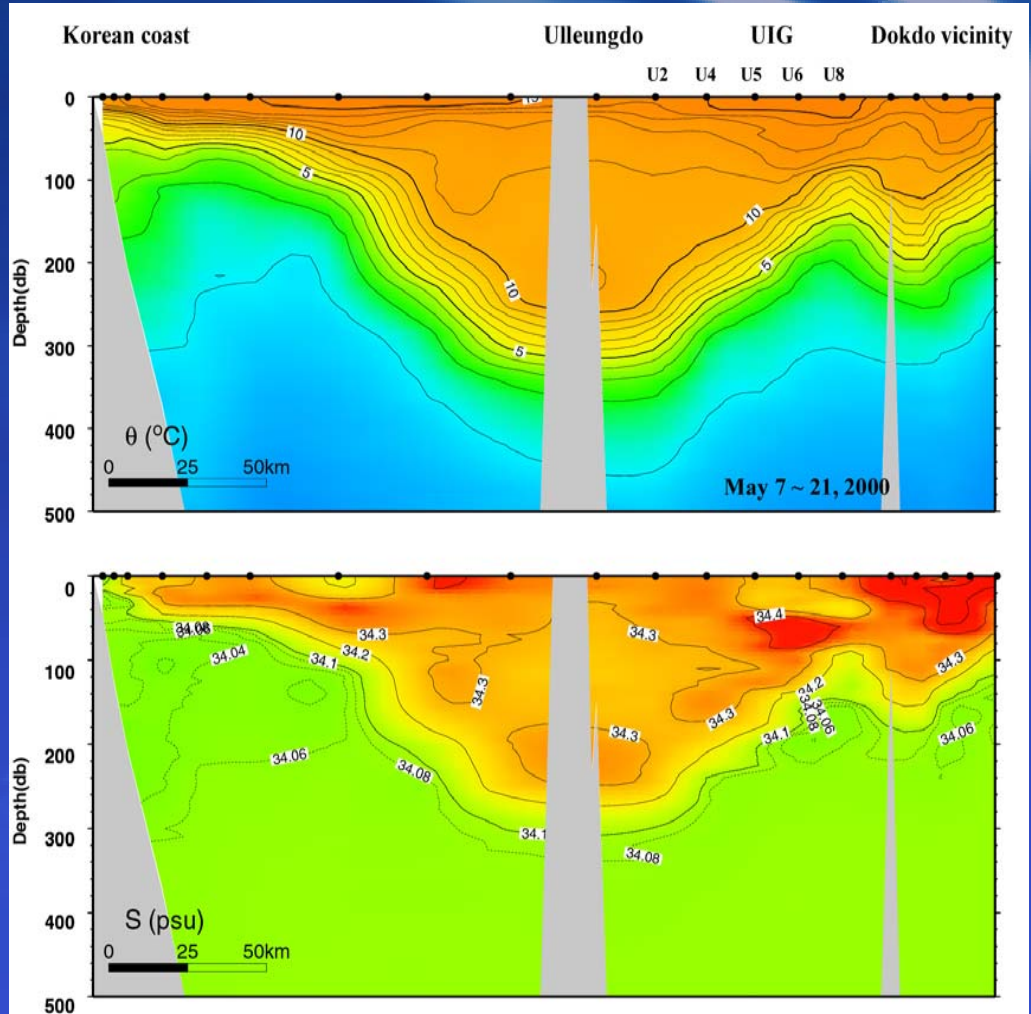
Deep water masses ($< 1^\circ\text{C}$)



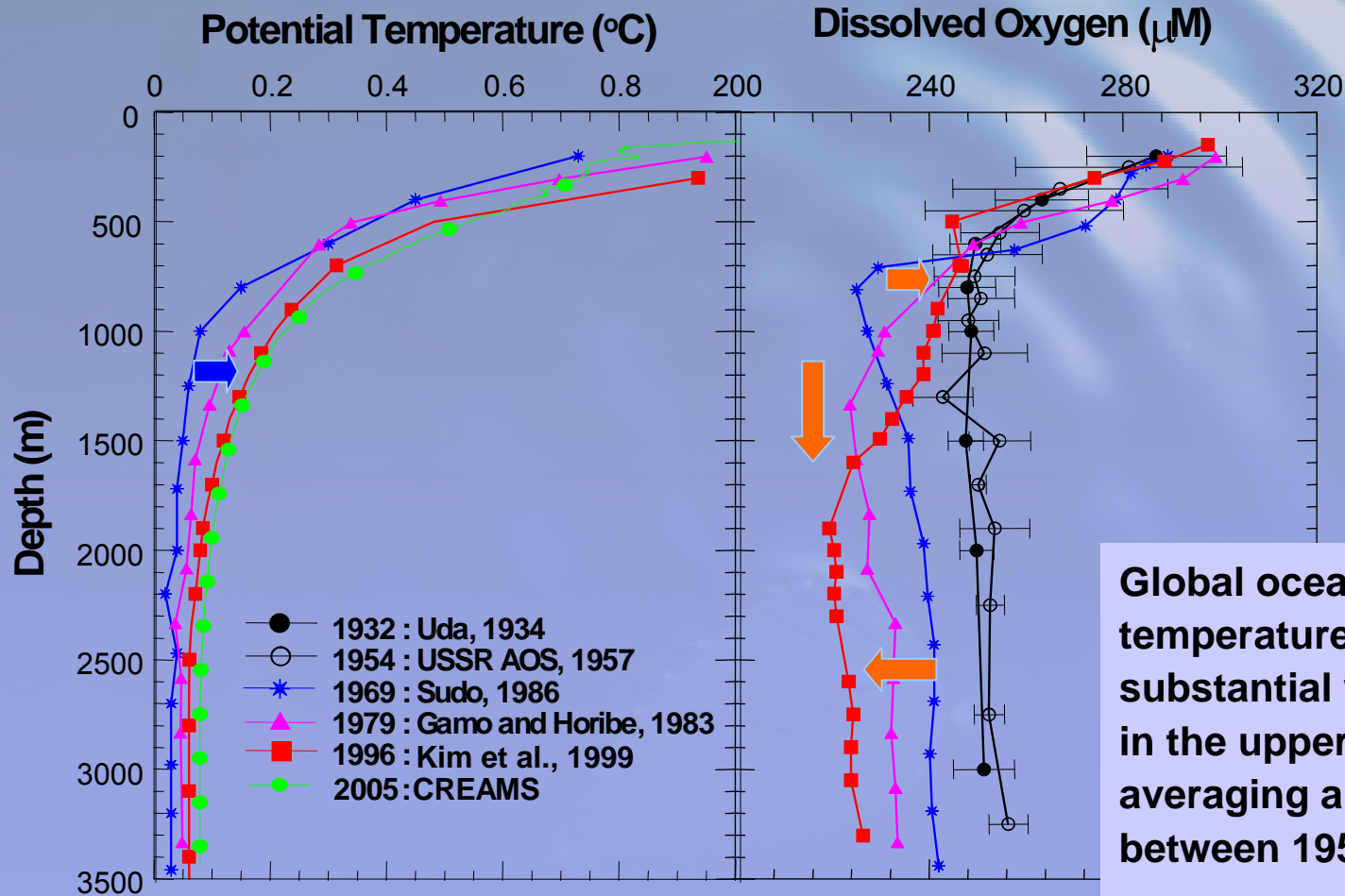
Regional setting: Eddies



Ulleung Warm Eddy



A Miniature Ocean in Change



Global ocean temperature change: substantial warming in the upper 3000m, averaging about 0.037°C between 1955 and 1998

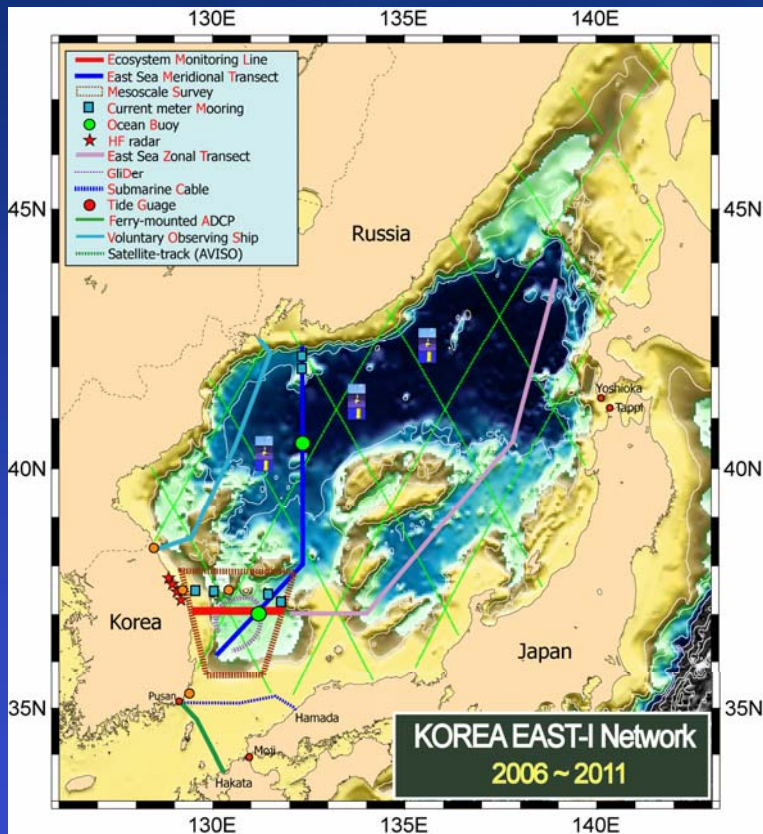
Levitus et al. (2005, GRL)



Brief History of International Programs

Before 1981 (1 st workshop)	Cooperative Study of the Kuroshio and Adjacent Regions (1965-1977)
1981-1992	Bilateral Collaboration (Korea/Tsushima Strait submarine cable voltage measurement)
1993-1997	CREAMS (Circulation Research of the East Asian Marginal Seas) Multi-national, multi-disciplinary collaboration
1998-2002	CREAMS II Japan/East Sea Program (USA/ONR)
2005	CREAMS/PICES Program under PICES (North Pacific Marine Science Organization) EAST-I Program (East Asian Seas Time-series: East/Japan Sea)

EAST(East Asian Seas Time-series) - I



- International collaborations
 - Joint surveys along meridional and zonal baselines; material flux measurements across the Korea Strait; joint workshops
- Eulerian time-series measurements
 - Volume transport monitoring; HF radar; coastal buoy and Super-Station; Volunteer observing ships; Moored observations
- Lagrangian measurements
 - Argo floats; Argos drifters; gliders



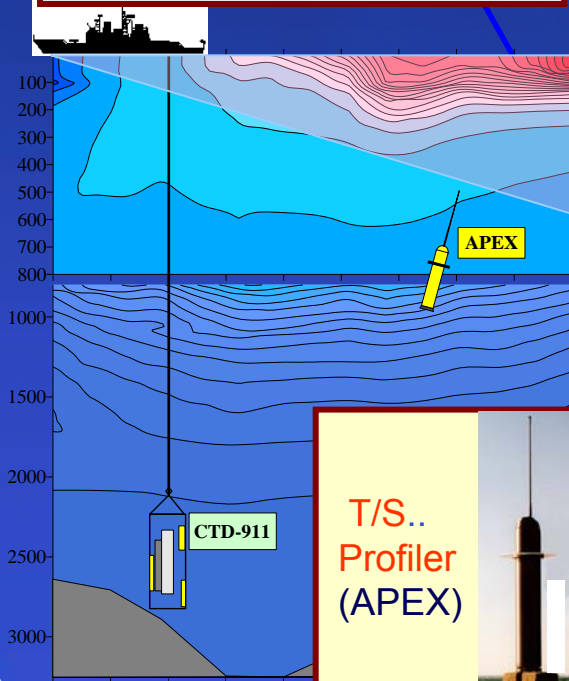
Research Tasks (EAST-I)

- ❖ Establishment of integrated ocean time-series system
- ❖ Ecosystem structure and variability in response to physical forcing
- ❖ Air-sea interaction, mixed layer dynamics and ecosystem response
- ❖ Monitoring and understanding the thermohaline circulation
- ❖ Carbon cycle and its response to climate change
- ❖ Role of straits in climate and ecosystem
- ❖ Physical-biological coupled modeling & future climate projection

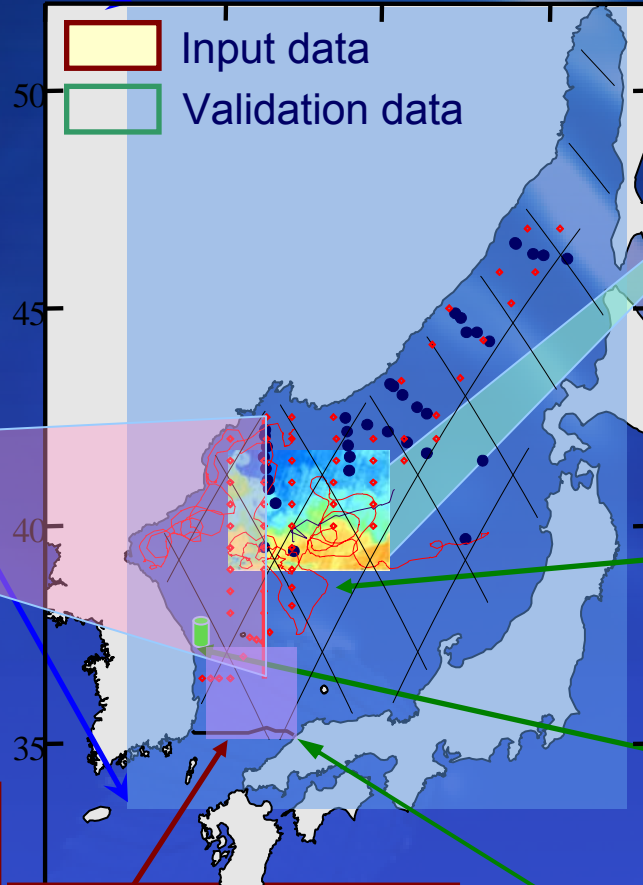
Observation Systems in the East/Japan Sea



Hydrographic Data
(CREAMS, JODC, KODC)



T/S.. Profiler
(APEX)



Inflow (Cable Voltage)

SST (NOAA)
SSH (T/P, ERS)
SSW (ECMWF)

Surface Current
(Surface Drifter)

Real-time Monitoring Buoy

140

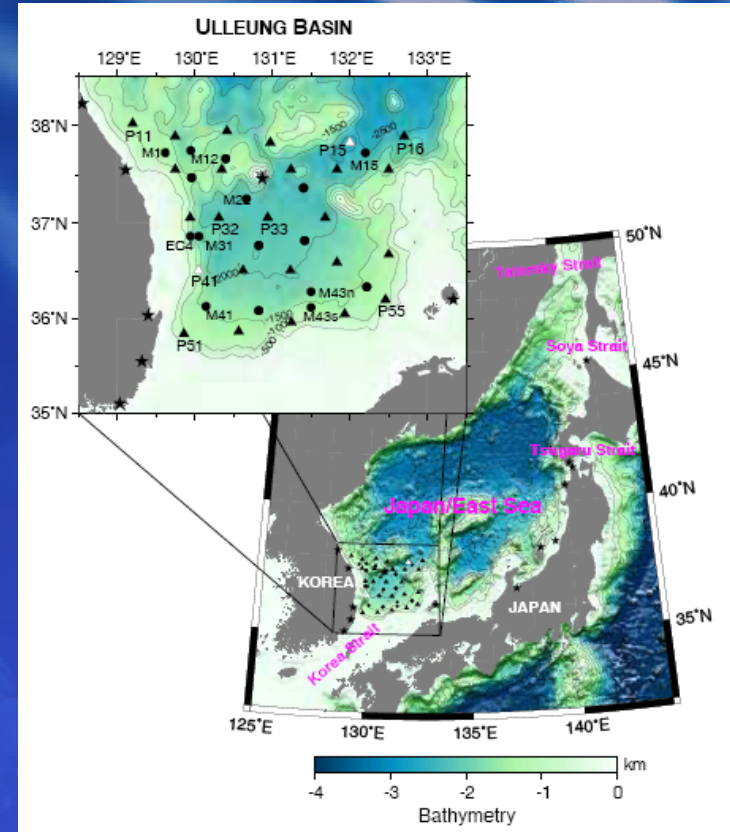
Temperature (PIES)

Highly-resolved Observation in the UB

ONR JES Program: URI, KORDI, KU

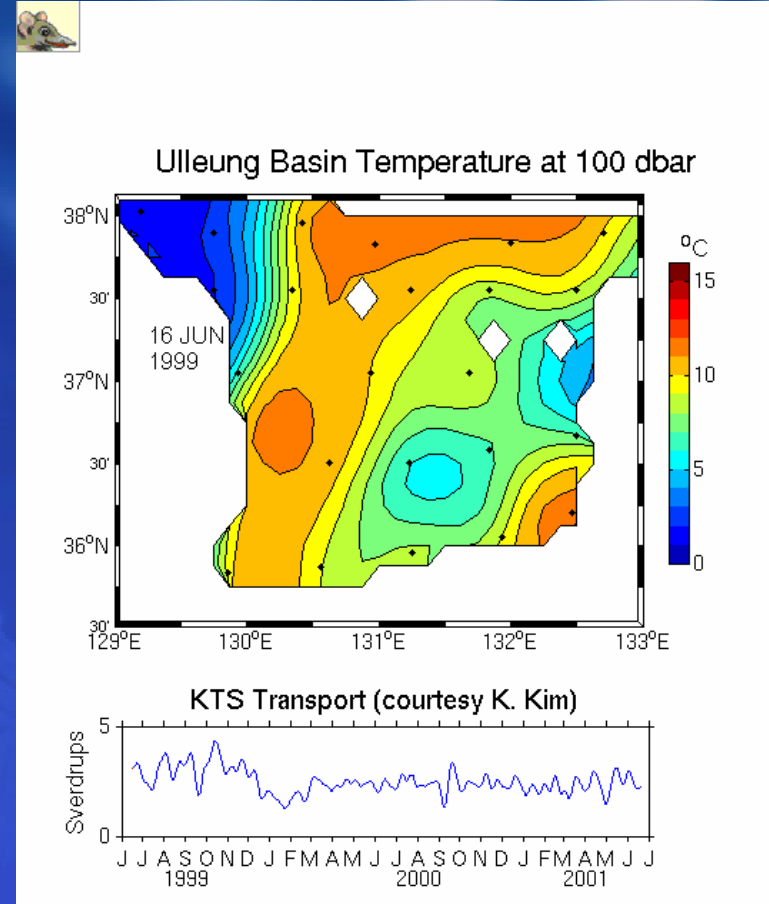
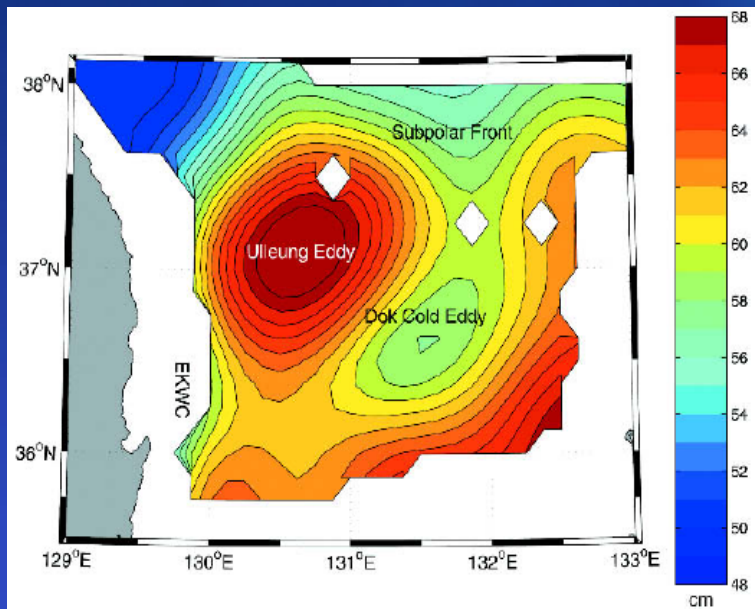
16 current meters, 23 pressure-gauge-equipped inverted echo sounders

Daily T & dynamic fields between June 1999 and June 2001



Regional setting: Circulation & Variability (UB)

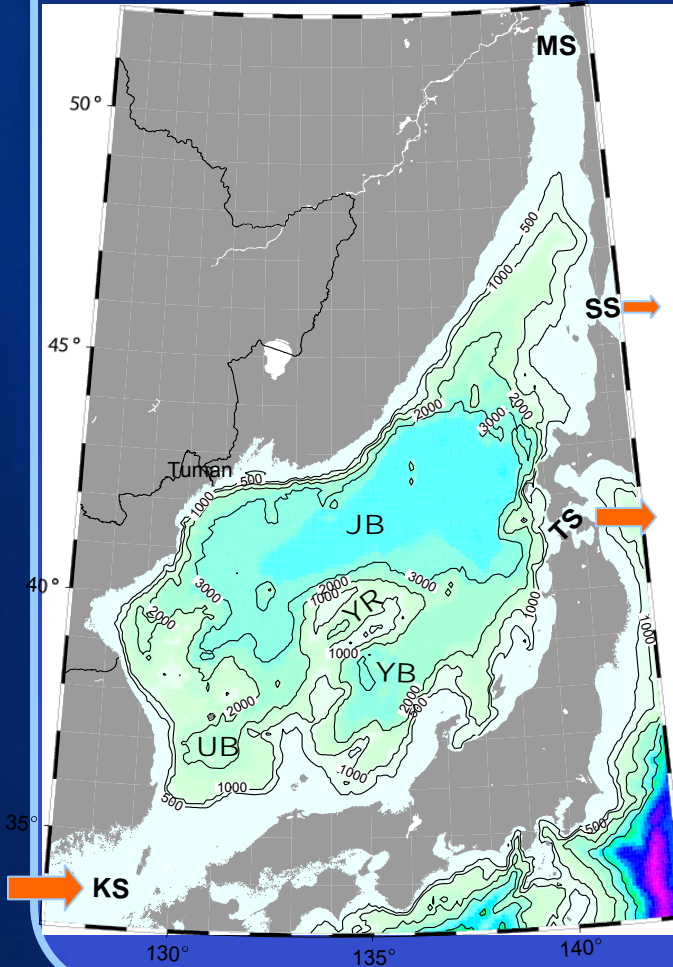
Mitchell et al. (2005); mean surface dynamic height



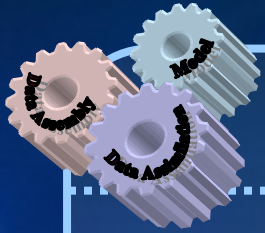
East Sea Regional Ocean Model (ESROM)

ESROM

Horizontal Domain (127.5 ~ 142.5 °E, 33.0 ~ 52.0 °N)
Horizontal resolution: 0.06~0.1°(zonal), 0.1° (meridional)
Modelling periods: 1993~2002



- ◆ Based on GFDL MOM3
 - ✓ Z-coordinate level model
 - ✓ Parallel Processing (MPI)
 - ✓ Hydrostatic and Boussinesq approximations
- ◆ Open Boundary Conditions
 - ✓ Barotropic velocity of inflow and outflow – Estimated from the transport estimated by submarine cable
 - ✓ Baroclinic structure of inflow – historical hydrography
- ◆ Surface Boundary Conditions
 - ✓ Heatflux - Calculated from meteorological variables by Bulk Formula
 - ✓ Saltflux - Restoring to observed SSS
 - ✓ Windstress - ECMWF
- ◆ Features
 - ✓ Explicit free surface
 - ✓ Smagorinsky SGS for momentum
 - ✓ Robert-Marshall Isoneutral SGS for tracers
 - ✓ KPP Vertical SGS Parameterization
 - ✓ Partial cell



Surface Boundary Condition

ESROM

Forced by monthly mean Surface Boundary Conditions and Open Boundary Conditions

Heatflux – Bulk Formula

$$Q_{net} = Q_{sw} - (Q_{sen} + Q_{lat} + Q_{lw})$$

$$Q_{sen} = \rho_a C_p^a C_h W_{10} (T_a - \theta_1)$$

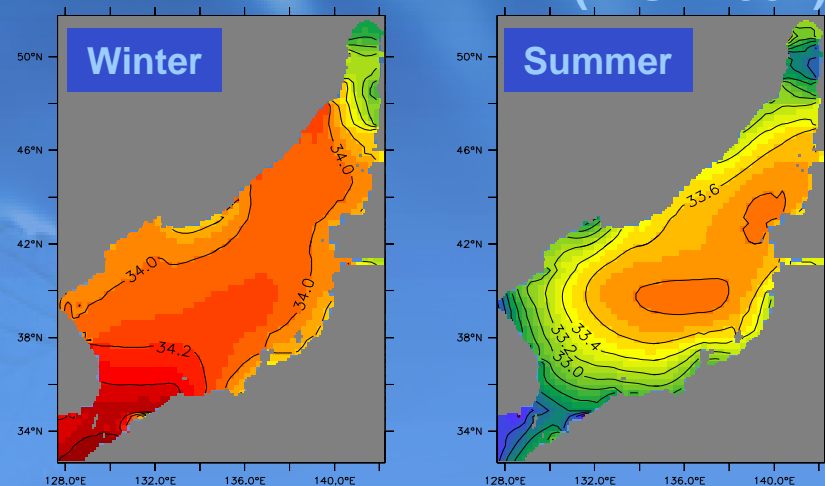
$$Q_{lat} = \rho_a L_e C_E W_{10} (q_a - q_1)$$

$$Q_{lw} = -\varepsilon \sigma_{SB} \left\{ T_a^4 \left[0.39 - 0.05(e_a)^{0.5} \right] F(c) + 4T_a^3 (\theta_1 - T_a) \right\}$$

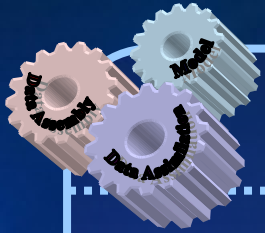
Saltflux – Restoring to SSS

$$S_{surf}^{\tau+1} = \gamma (S_{obs} - S_{surf}^{\tau})$$

(WOA2001)

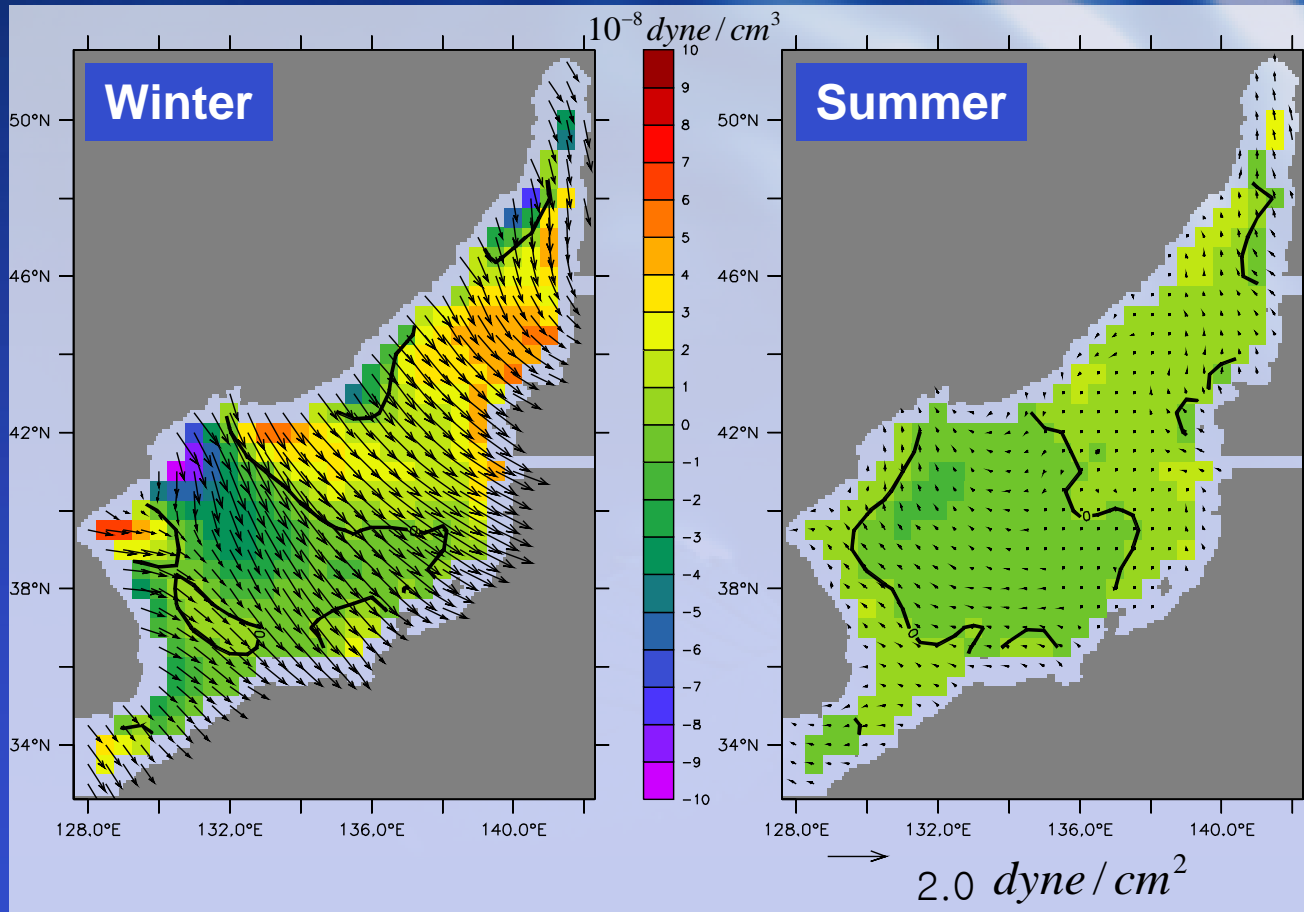


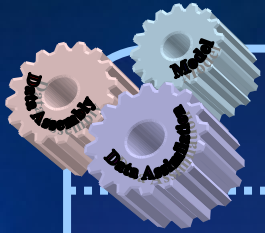
Large, William G., et. al., 1997, Sensitivity to Surface Forcing and Boundary Layer Mixing in a Global Ocean Model : Annual-Mean Climatology, J. of Phys. Oceano., vol. 27, 2418-2447



Surface Boundary Condition

Windstress (ECMWF)





Open Boundary Conditions

ESROM

- Radiation condition for the tracers and barotropic velocity

$$\frac{\partial \phi}{\partial t} + C_x \frac{\partial \phi}{\partial x} + C_y \frac{\partial \phi}{\partial y} = 0$$

$$C_x = \frac{\partial \phi}{\partial t} \frac{\partial \phi / \partial x}{(\partial \phi^2 / \partial x^2) + (\partial \phi^2 / \partial y^2)}$$

$$C_y = \frac{\partial \phi}{\partial t} \frac{\partial \phi / \partial y}{(\partial \phi^2 / \partial x^2) + (\partial \phi^2 / \partial y^2)}$$

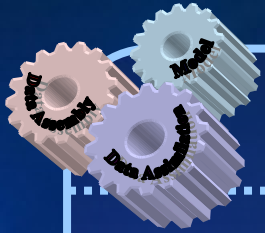
- An additional nudging term is added for the influxes

$$\frac{\partial \phi}{\partial t} + C_x \frac{\partial \phi}{\partial x} + C_y \frac{\partial \phi}{\partial y} = -\frac{1}{\tau} (\phi - \phi^{ext}) \quad \begin{array}{l} \tau = \tau_{out} \text{ if } C_x > 0 \\ \tau = \tau_{in} \text{ and } C_x = C_y = 0 \text{ if } C_x < 0 \end{array}$$

- Volume constraint

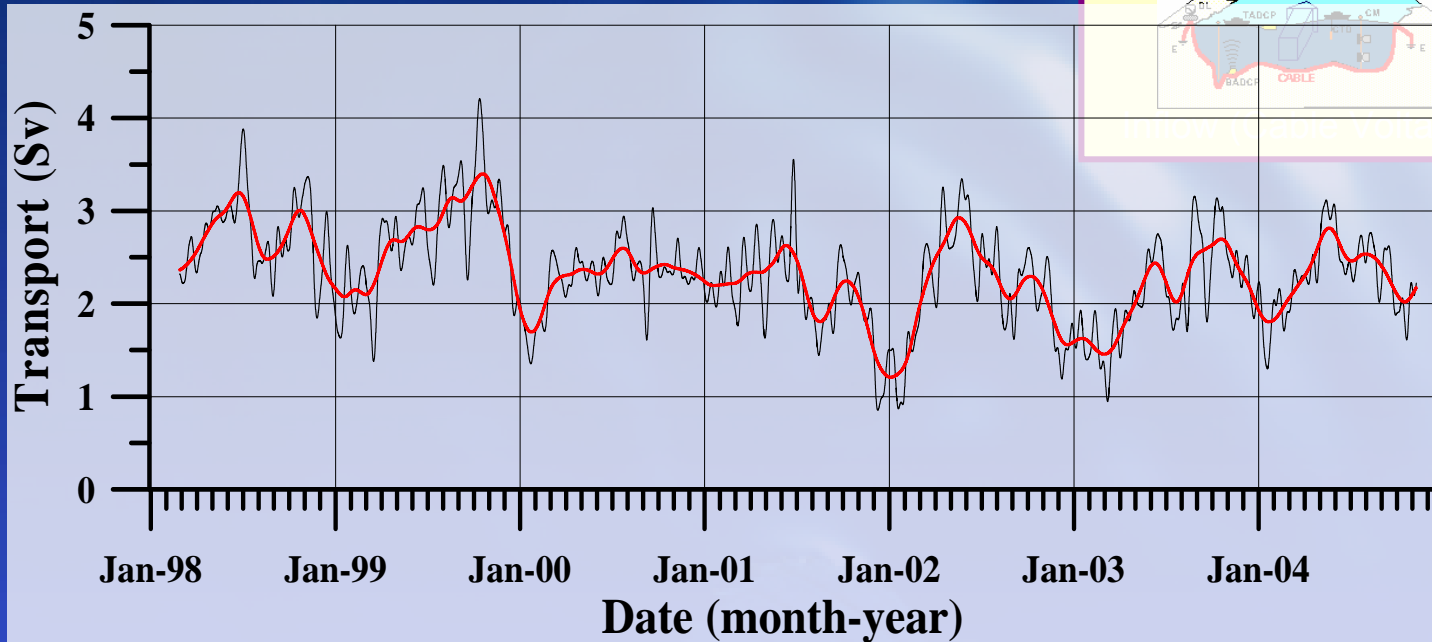
$$\frac{dV}{dt} = \frac{d}{dt} \left[\iiint_V dV \right] = \iint_{S_b} \vec{u} \cdot \vec{n} dS = \int_{L_b} h \vec{u} \cdot \vec{n} dL$$

Marchesiello, P., McWilliams, J.C., and Shchepetkin, A. (2001) Open boundary conditions for long-term integration of regional oceanic models, *ocean modeling*, 3: 1-20.



Open Boundary Conditions

ESROM



Volume transport through the Korea Strait by a submarine cable between Pusan and Hamada



Theoretical Implementation

Weaver and Courtier (2001)

- A central task in the development of a statistical data assimilation

Estimation of background error covariance

- Size of background error covariance matrix

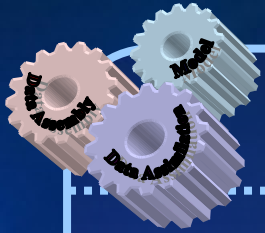
: $\sim 5 \times 10^{11}$ (x 8 byte) = 4,000 Gbyte – **neither estimated completely nor even stored explicitly**



Modeling B matrix as a sequence of operators.



Correlation modeling on the sphere using a generalized diffusion equation



Theoretical Implementation

- ❑ Variational assimilation system with atmospheric models

Background error covariance - Correlation functions in terms of a spherical harmonic expansion

It is not practical for the ocean due to **lateral boundary**

- ❑ Assimilation system with oceanic model

Lorenz (1992, 1997) and Parrish et al. (1997) : Recursive grid-point filters (UKMO)

Derber and Rosati (1989) : Iterative Laplacian grid-point filter (NCEP)

- 😊 Very efficient and flexible for geographical variations
- - Limited flexibility in the **shape of the correlation function**
difficult to make **anisotropic**

❑ Objectives : 3D univariate correlation models **numerically efficient and sufficiently general**; correlation functions with different shape (not just Gaussian), geographically variable length-scale, horizontal/vertical non-separability, and 3D anisotropy.

3D correlation model

Vertical correlation model

$$L_R^v = \left\{ I - \sum_{r=1}^R \kappa_r \Delta t_v (-D^v)^r \right\}^{M_v}, \text{ Diffusion equation}$$

3D covariance operator

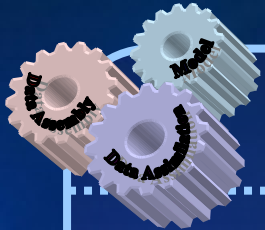
$$\begin{aligned} L_R^v W_v^{-1} L_P^h W_h^{-1} &= L_R^{v/2} W_v^{-1} L_R^{T/2} L_P^{h/2} W_h^{-1} L_P^{T/2} \\ &= L_R^{v/2} L_P^{h/2} W_h^{-1} L_P^{T/2} L_R^{T/2} \end{aligned}$$

$$C_\alpha^{1/2} = \Lambda L_R^{v/2} L_P^{h/2} W_h^{-1/2}, \quad C_\alpha^{T/2} = W_h^{-1} L_P^{T/2} L_R^{T/2}$$

Sequence of operations for $C_\alpha^{1/2}$, Correlation model

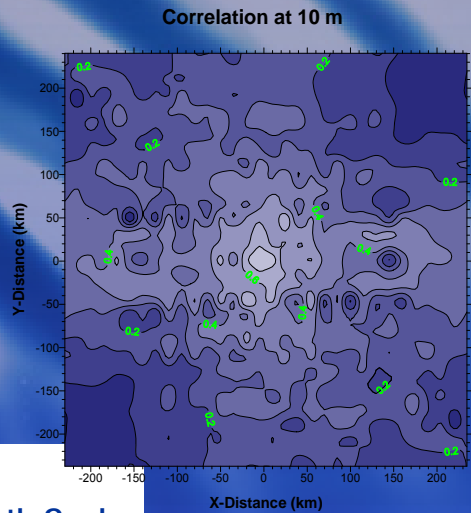
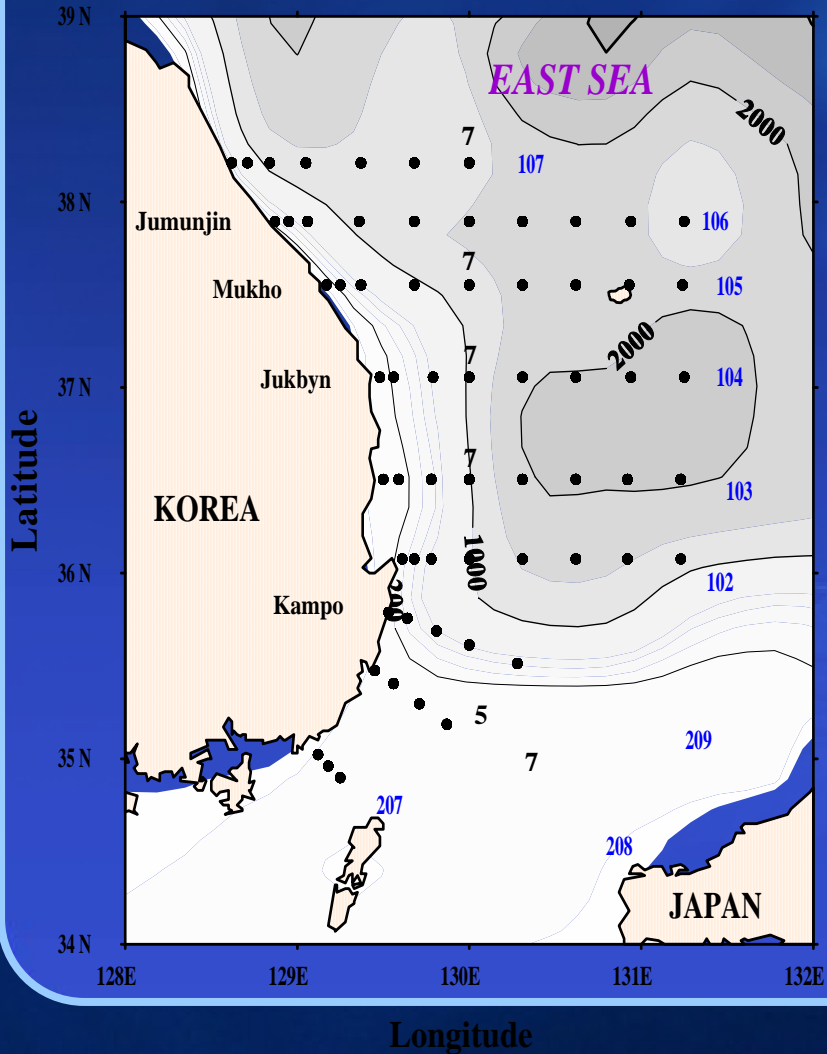
- (i) Multiply each element of the input vector by the inverse of the square root of its associated volume element
- (ii) Perform $M_h/2$ integration steps of the horizontal diffusion equation
- (iii) Perform $M_v/2$ integration steps of the vertical diffusion equation
- (iv) multiply each element of the filtered vector by its corresponding normalization factor

Applied in reverse order for $C_\alpha^{T/2}$ with adjoint code of the diffusion equation

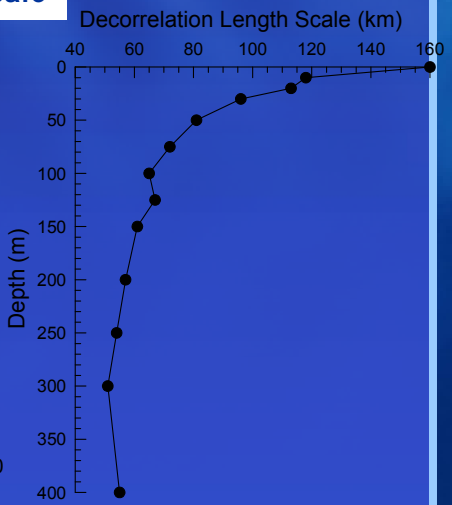
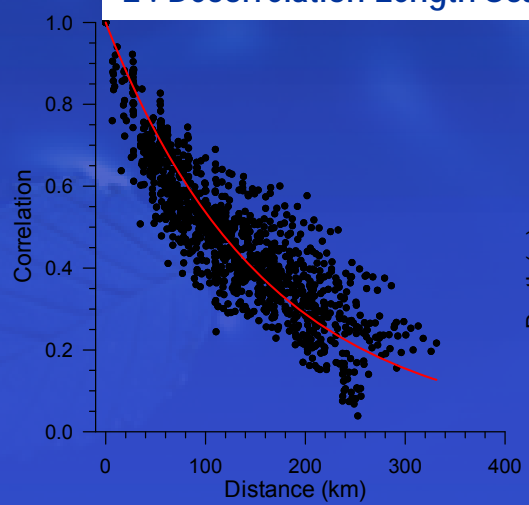


De-Correlation Length Scale

Characteristics of the hydrography taken by the NFRDI, Korea

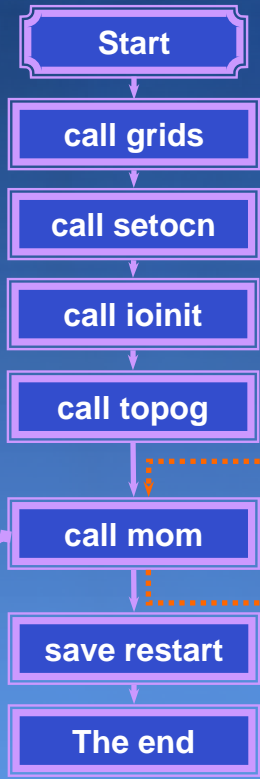


$fn(r) = \text{Exp}(-r/L)$
L : Decorrelation Length Scale

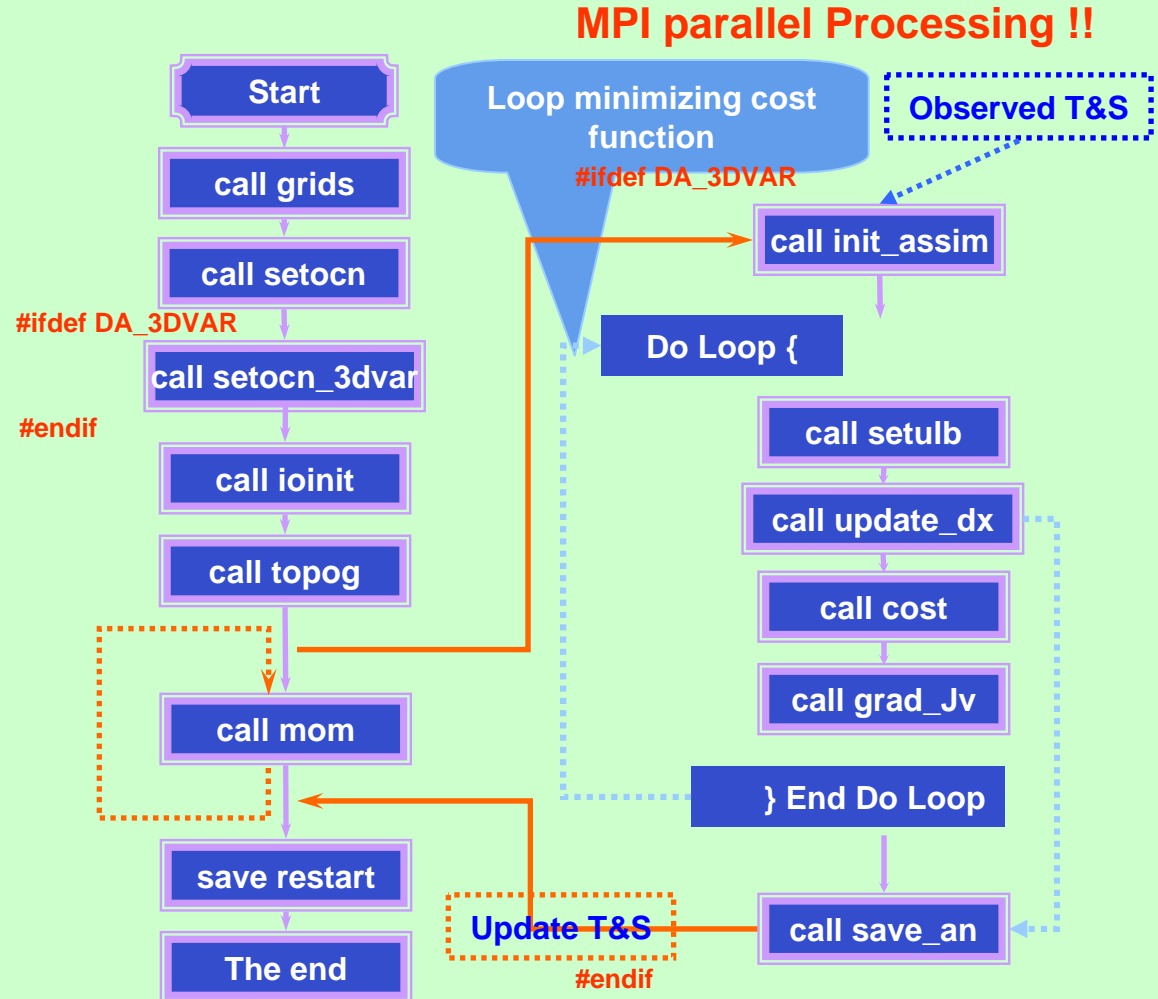


Horizontal Decorrelation Length Scale : 77 km
Vertical Decorrelation Length Scale : 77 m

Ocean Model Structure



Ocean Model & D.Assimilation Structure



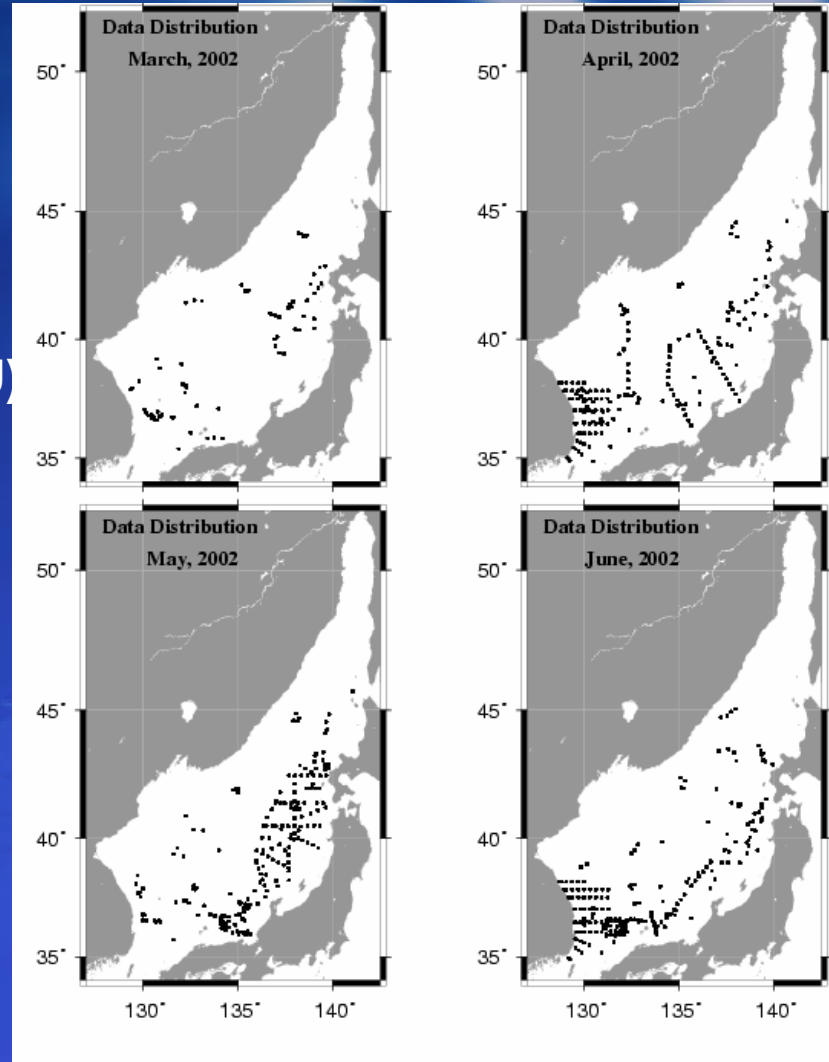
Ocean model

Data distribution

3-DVar

Reanalysis with

1. SST Satellite image
2. Temperature of CREAMS(SNU)
3. Temp. of NFRDI
4. Temp. of JODC
5. Temp. taken by ARGO floats





Theoretical Implementation

Cooper and Haines (1996)

Surface data assimilation problem – Requirement of a rearrangement of water parcels in space without modifying their T,S properties or their potential vorticity.

Hydrostatic connection between Δp_s and subsurface pressure updates,

$$\Delta p(z) = \Delta p_s + g \int_z^0 \Delta \rho dz$$

If we set $\Delta p(z = -H) = 0$ as a bottom constraint, this will ensure that the bottom pressure and current distribution (through geostrophy) are not altered.

This bottom constraint gives the relationship

$$g \int_0^{-H} \Delta \rho dz = \Delta p_s$$


the change in weight of the entire water column should compensate for the change in surface pressure observed by the altimeter

Assimilating Sea Surface Height


Cooper and Haines (1996)

Sea Surface  $\Delta p_s = \rho_s g \eta$

Isopycnic Surface

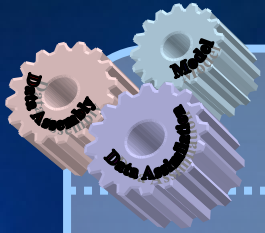


$$g \int_z^0 \Delta \rho dz$$



$$\Delta p(z = -H) = \Delta p_s + g \int_{-H}^0 \Delta \rho dz$$

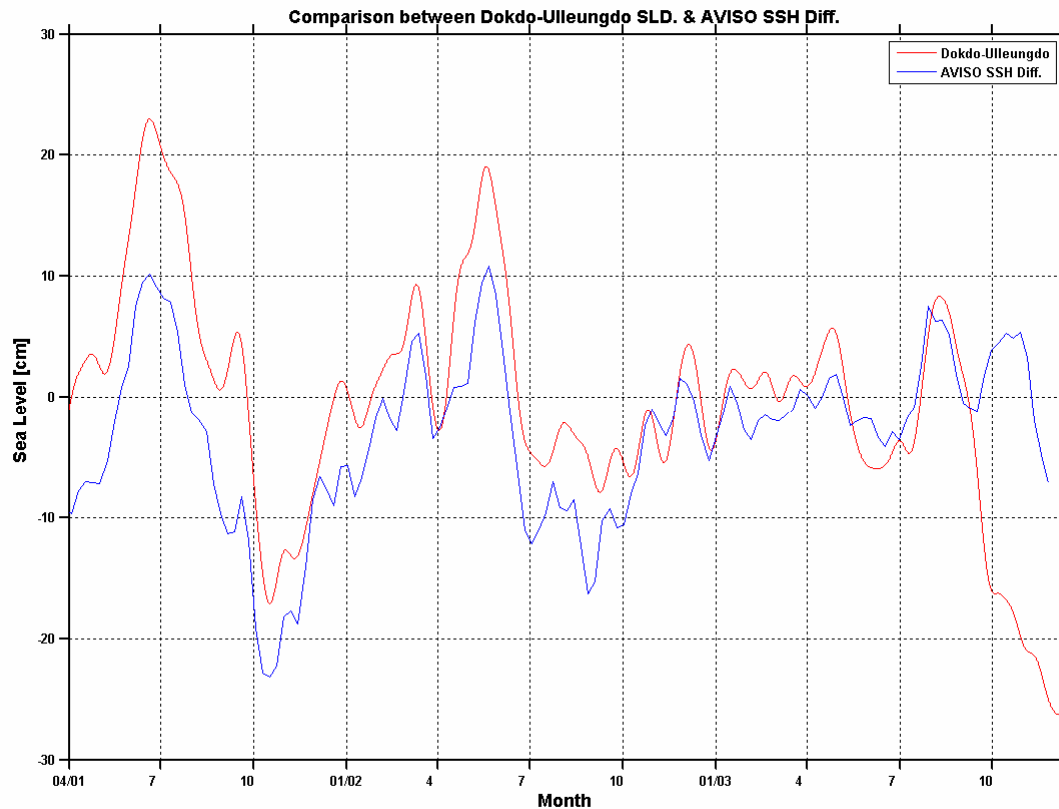
No Change of the Bottom Pressure !!!



Using AVISO Product

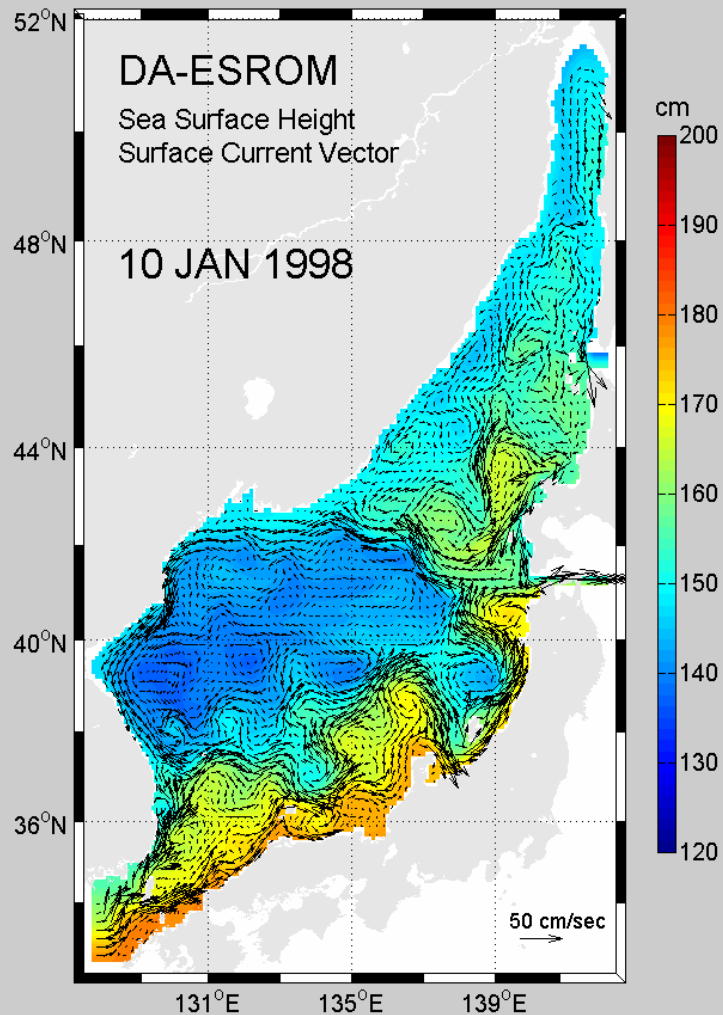
3-DVar

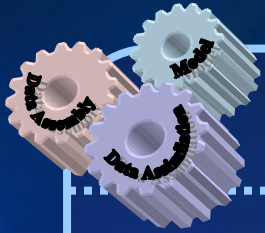
- ✦ Sea Level at Ulleung and Dok Islands
- ✦ Nearest point of the AVISO from Obs.



Surface current and Height (Model)

3-DVar

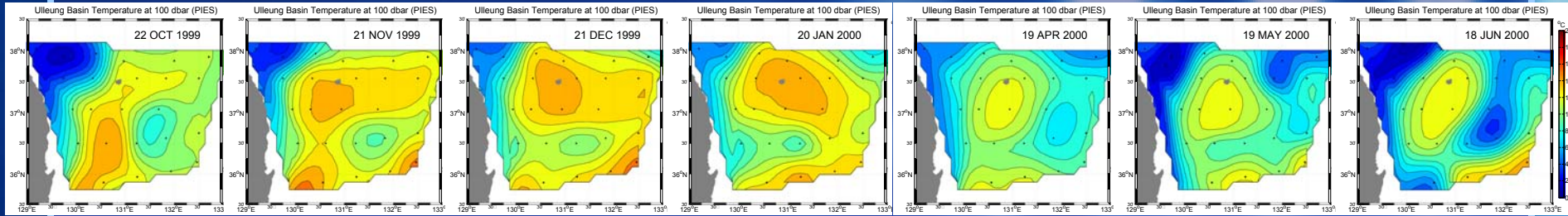




Comparison with Observation (100m)

Validation

PIES measurement



Oct., 1999

Nov.

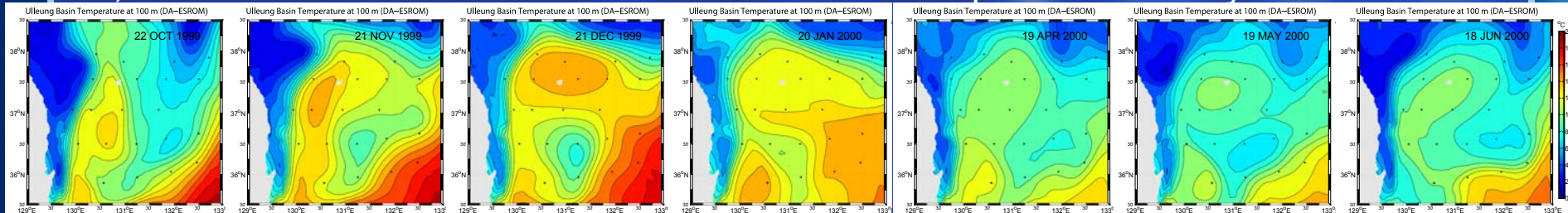
Dec.

Jan. 2000

Apr.

May.

Jun.

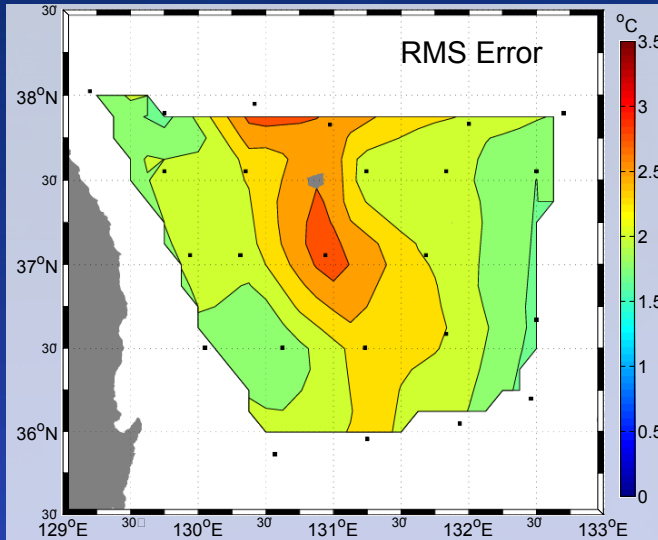


Reanalysis Product by DA-ESROM

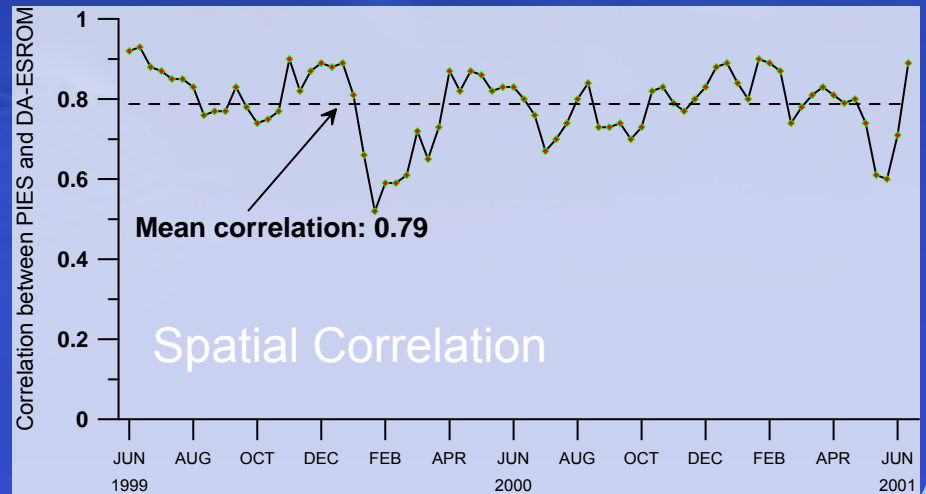
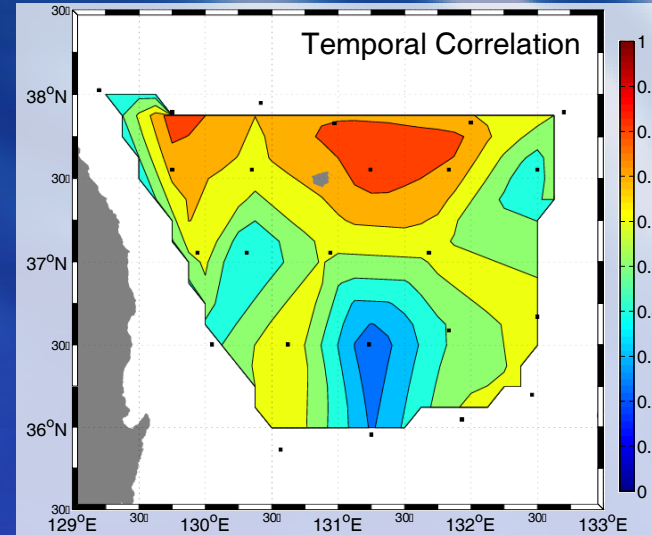
Comparison with Observation (100m)

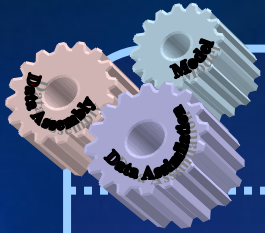
Validation

Spatio-temporal correlation



RMS Error between PIES measurements and reanalysis



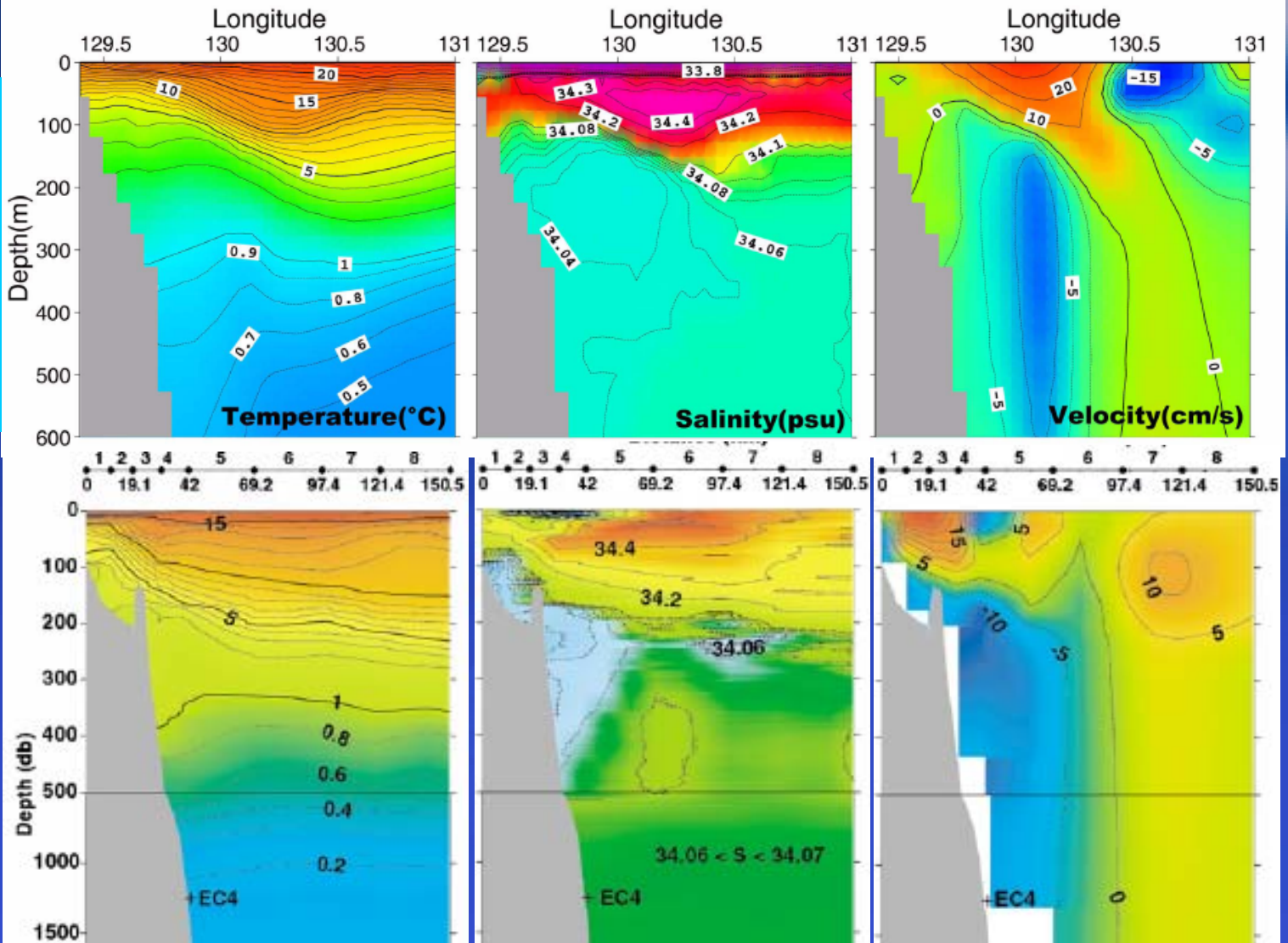


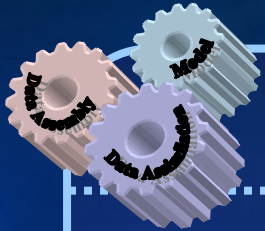
Model & Data Comparison at 36.8°N (May, 2000)

Validation

DA-ESROM Ver 2.0

Observation (Chang et al. 2002)

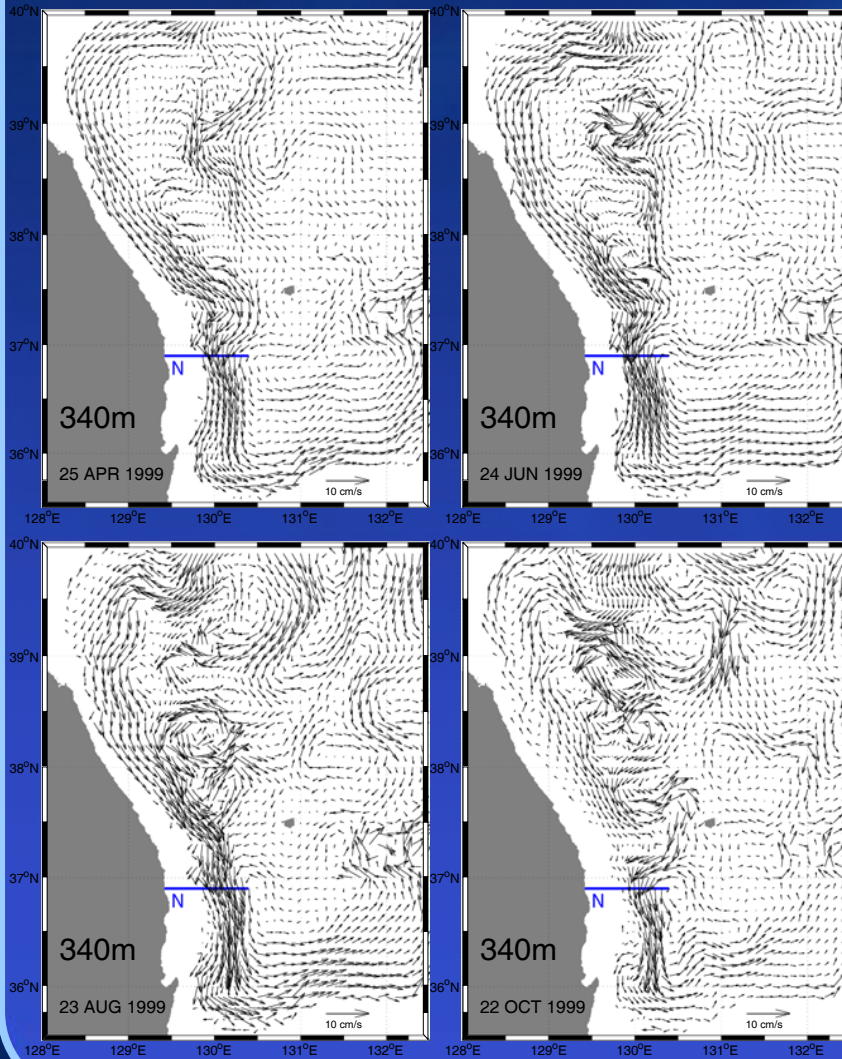




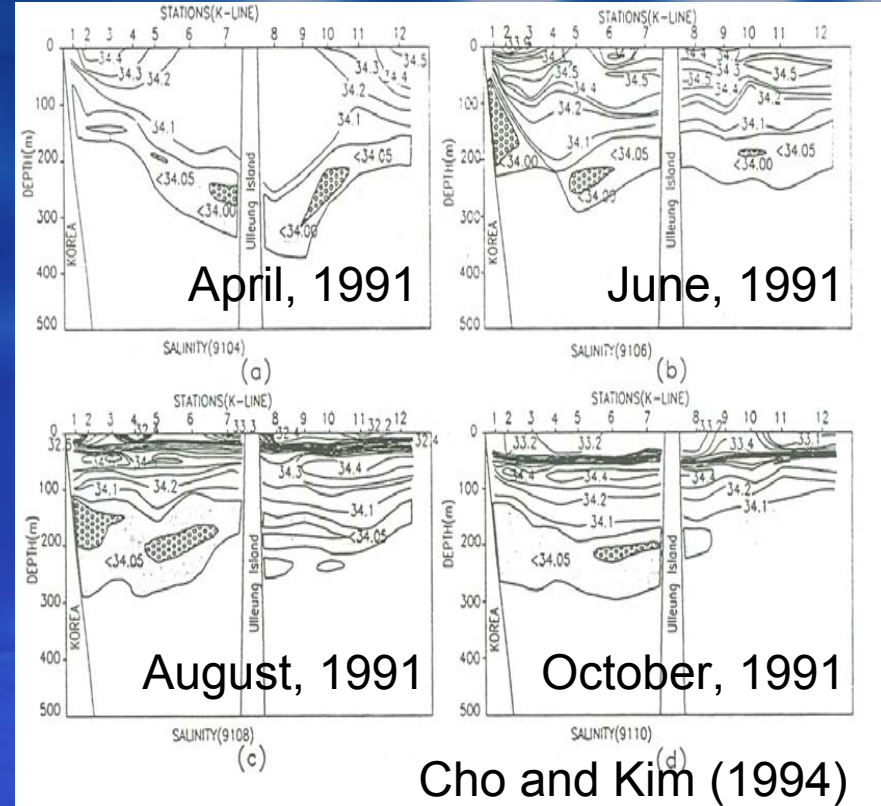
Strengthening of NKCC in summer

Validation

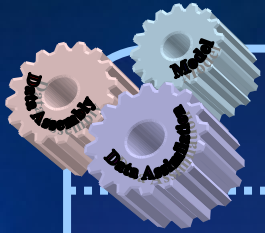
Reanalysis (DA-ESROM)



Salinity section (Observation)

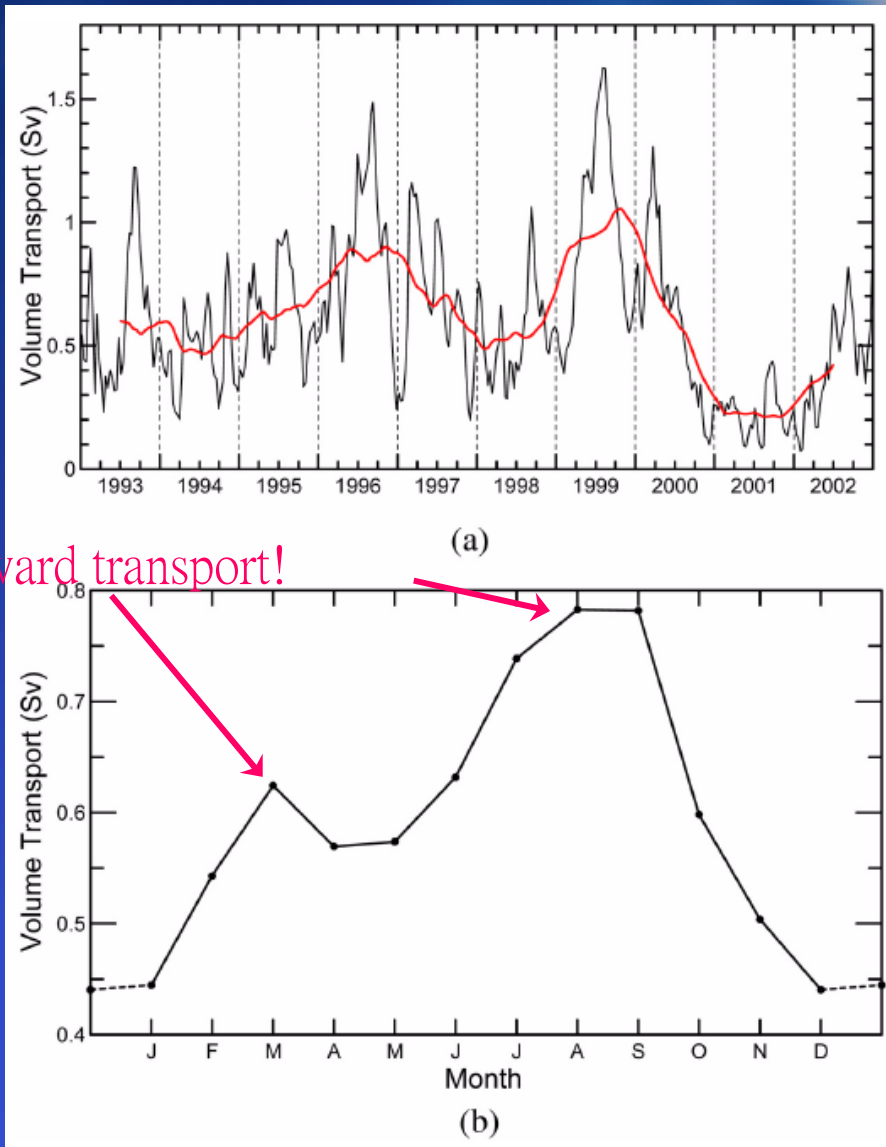


- **Southward advection** of the **Low Salinity Minimum Water (North Korean Cold Water)** in **Summer**. (Kim and Kim, 1983)



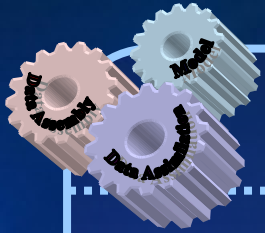
Seasonal and Interannual variation

Validation



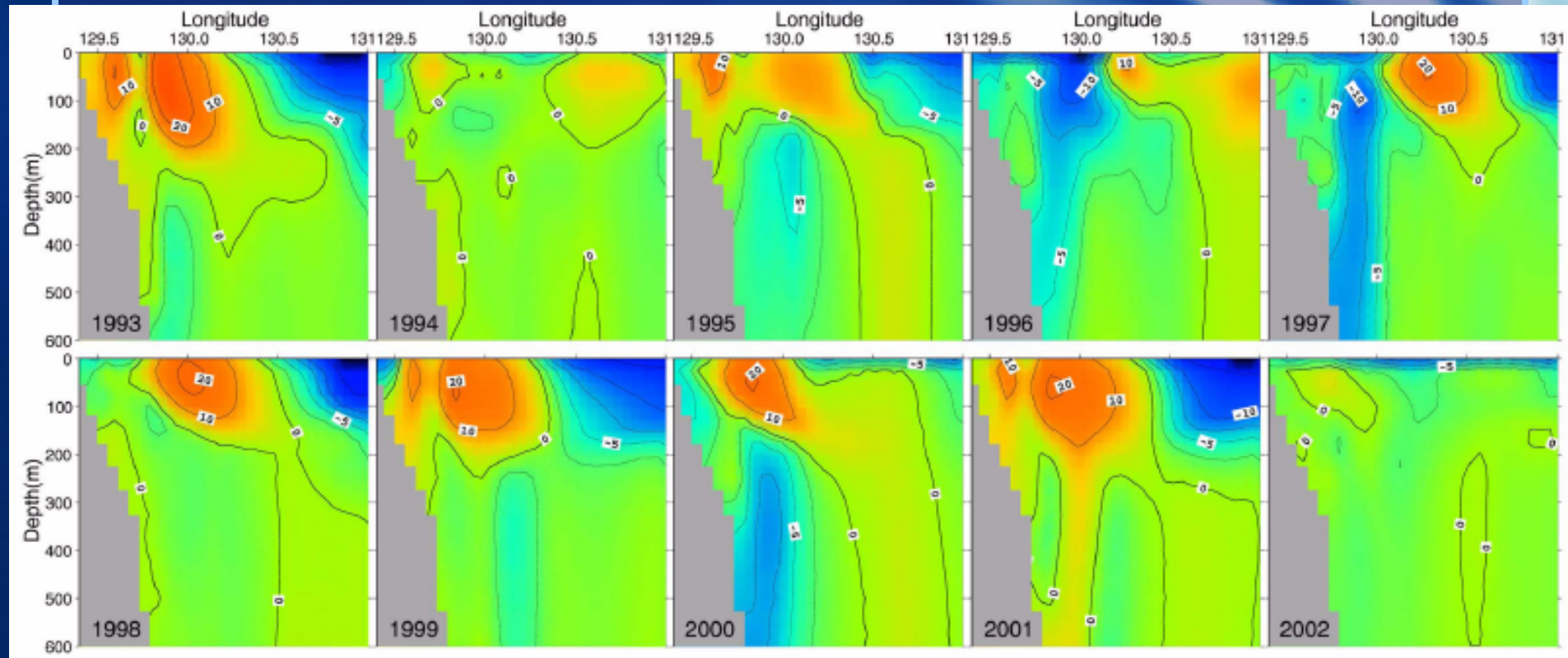
Maximum southward transport!

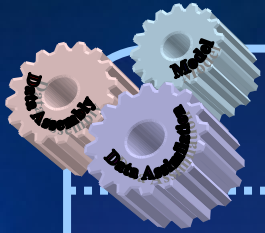
Volume Transport of NKCC across N line



Interannulation variation of NKCC in March

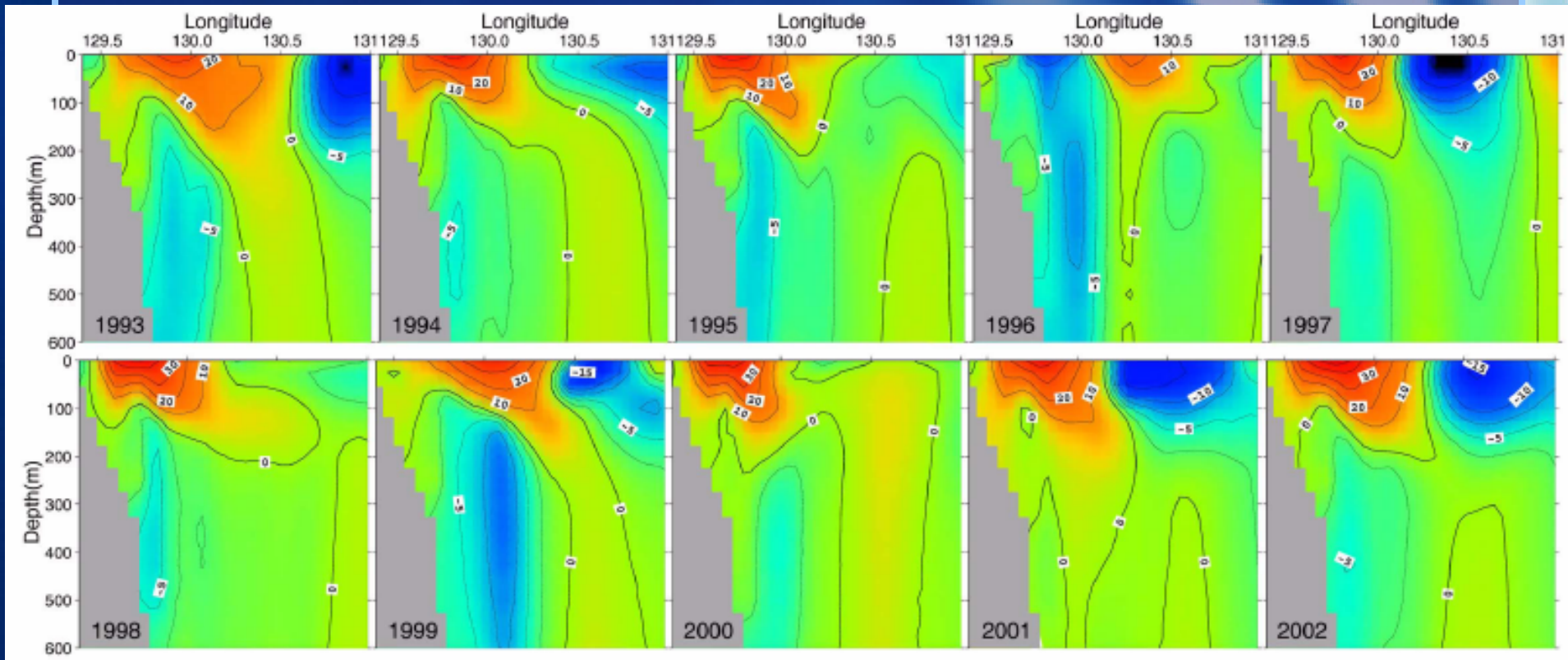
Validation

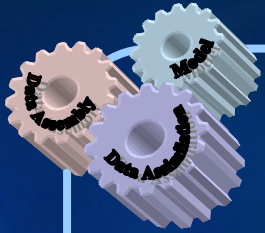




Interannulation variation of NKCC in August

Validation





4

Future Work : Ensemble Kalman Filter



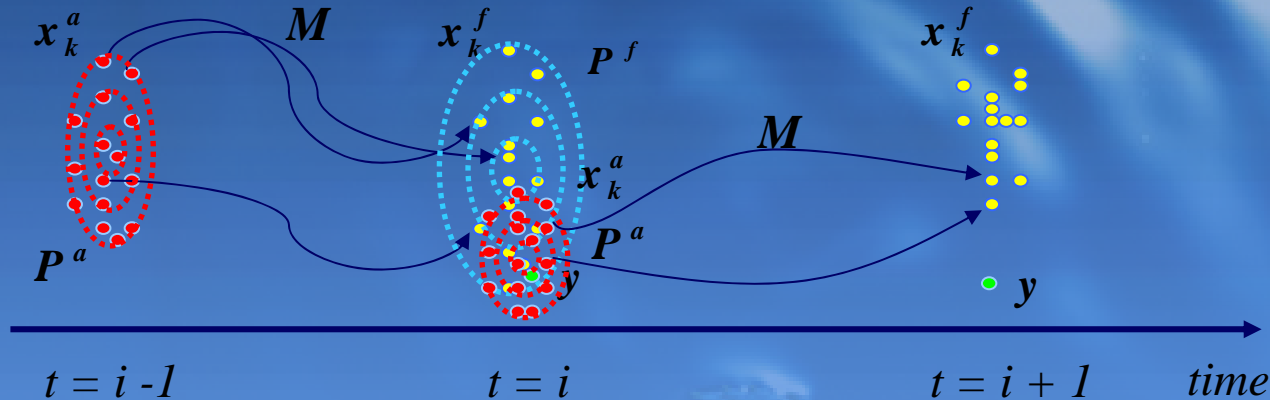
Introduction of Ensemble Kalman Filter

EnKF

P.L. Houtekamer and Herschel L. Mitchell (2001)

$$P^f(t=i) \approx \Psi^f(t=i) \Psi^{fT}(t=i) : [N \times N_e][N_e \times N]$$

$$x_k^a = x_k^f + \Psi^f \Psi^{fT} H^T (H \Psi^f \Psi^{fT} H^T + R)^{-1} (y - H x_k^f), k = 1, 2, \dots, N_e$$



Merit

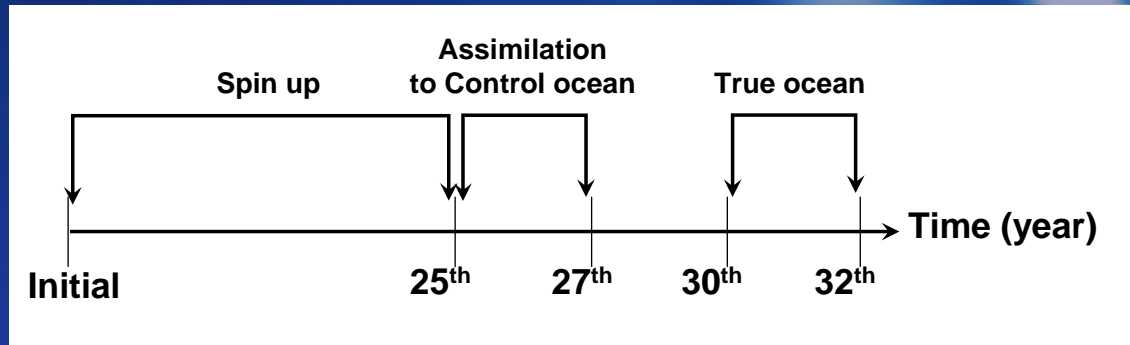
- Direct calculation of background error covariance from ensemble numerical models
- intuitive multi-variate background error covariance

Weak point

- Rank deficiency for not enough ensembles

Sensitivity Test (Twin Experiment)

EnKF



Experiment Design

	Num. of Ens. Mem.	Horizotal Local.	Vertical Local.	Cov. Inflation	SST Assim.	SSH Assim.	etc
E32	32	O	O	O	O	O	Success
REF	16	O	O	O	O	O	Success
HNLC	16	X	O	O	O	O	Overflow
VNLC	16	O	X	O	O	O	Unstable
CNINF	16	O	O	X	O	O	Success
ASSH	16	O	O	O	X	O	Success



True vs. Model

EnKF

Initial State

6 Month

12 Month

18 Month

24 Month

True Field

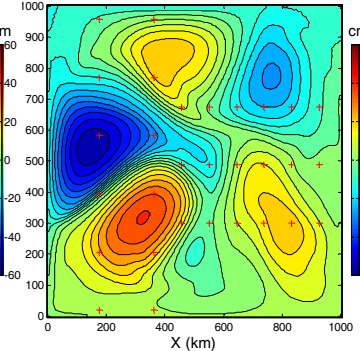
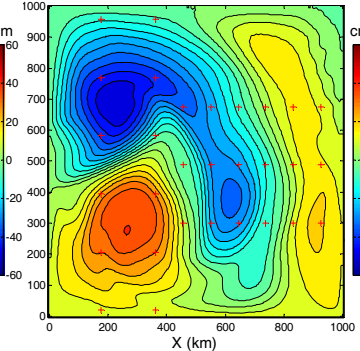
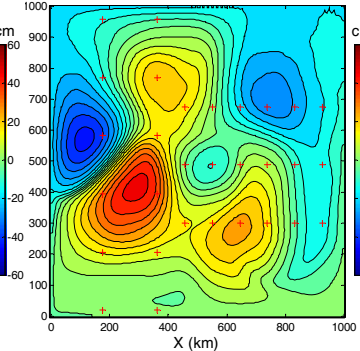
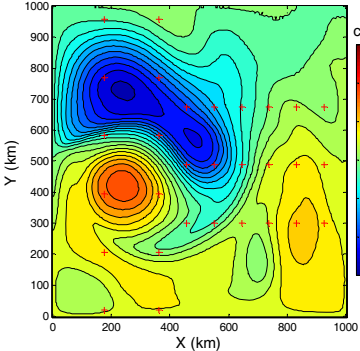
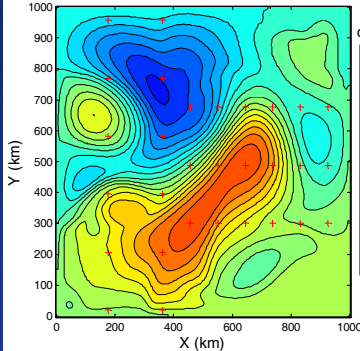
Sea Surface Elevation

Sea Surface Elevation

Sea Surface Elevation

Sea Surface Elevation

Sea Surface Elevation



Exp. REF

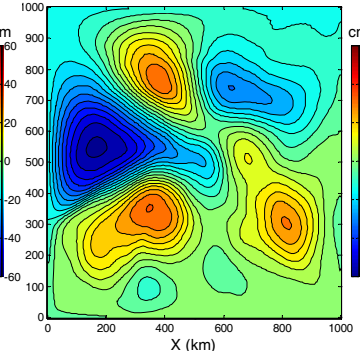
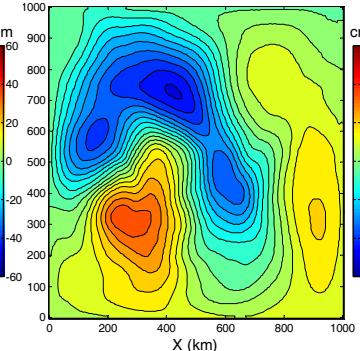
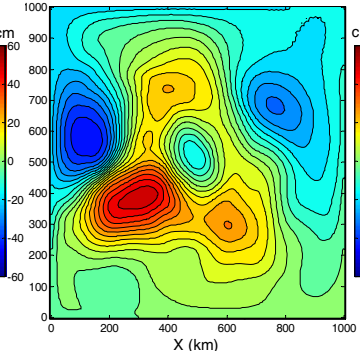
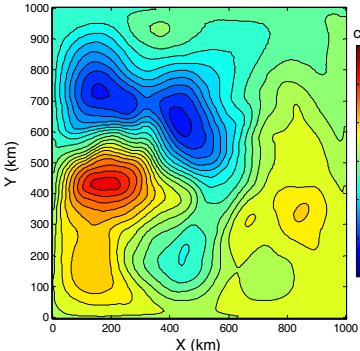
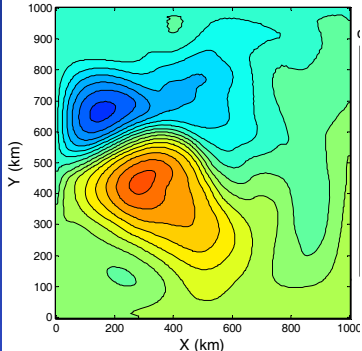
Sea Surface Elevation

Sea Surface Elevation

Sea Surface Elevation

Sea Surface Elevation

Sea Surface Elevation



Exp. E32

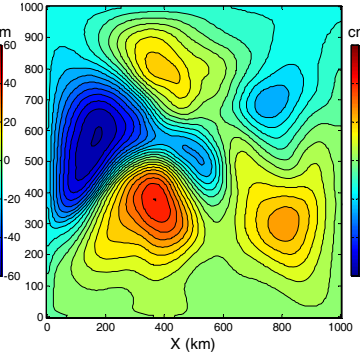
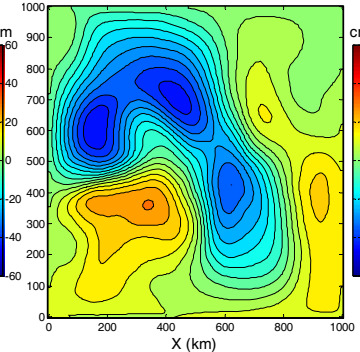
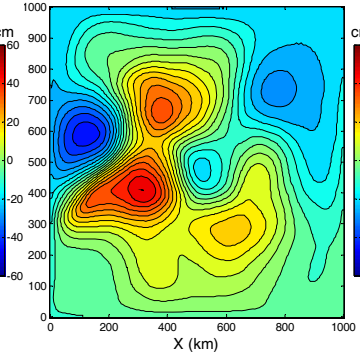
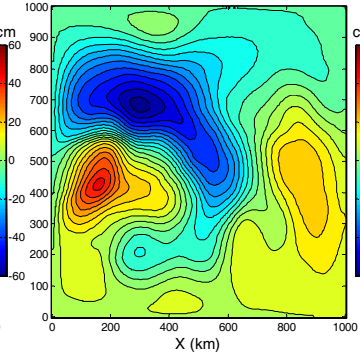
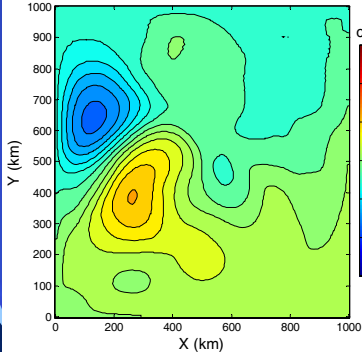
Sea Surface Elevation

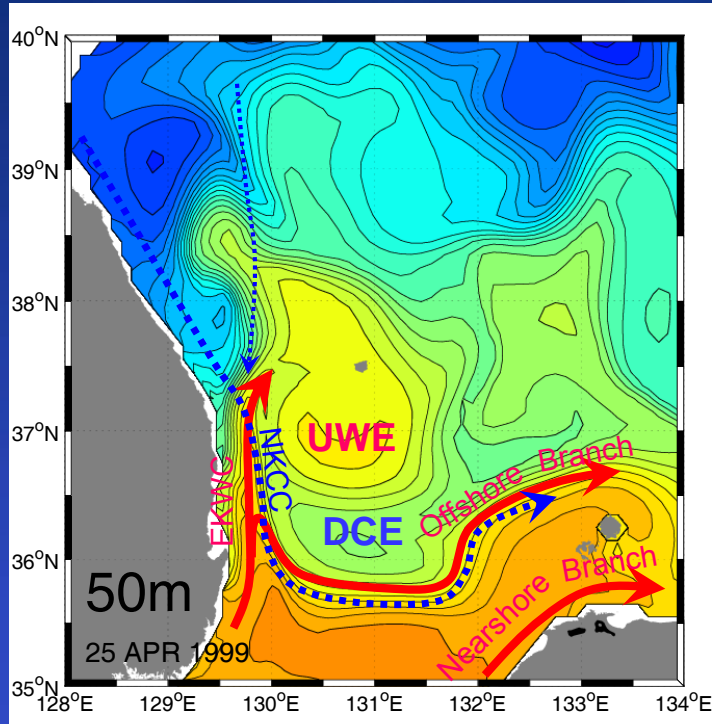
Sea Surface Elevation

Sea Surface Elevation

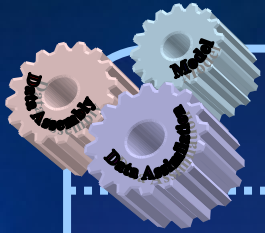
Sea Surface Elevation

Sea Surface Elevation



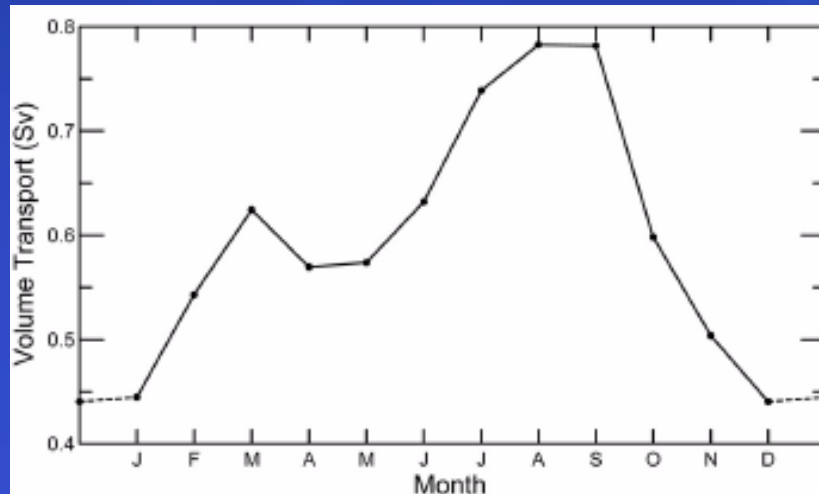
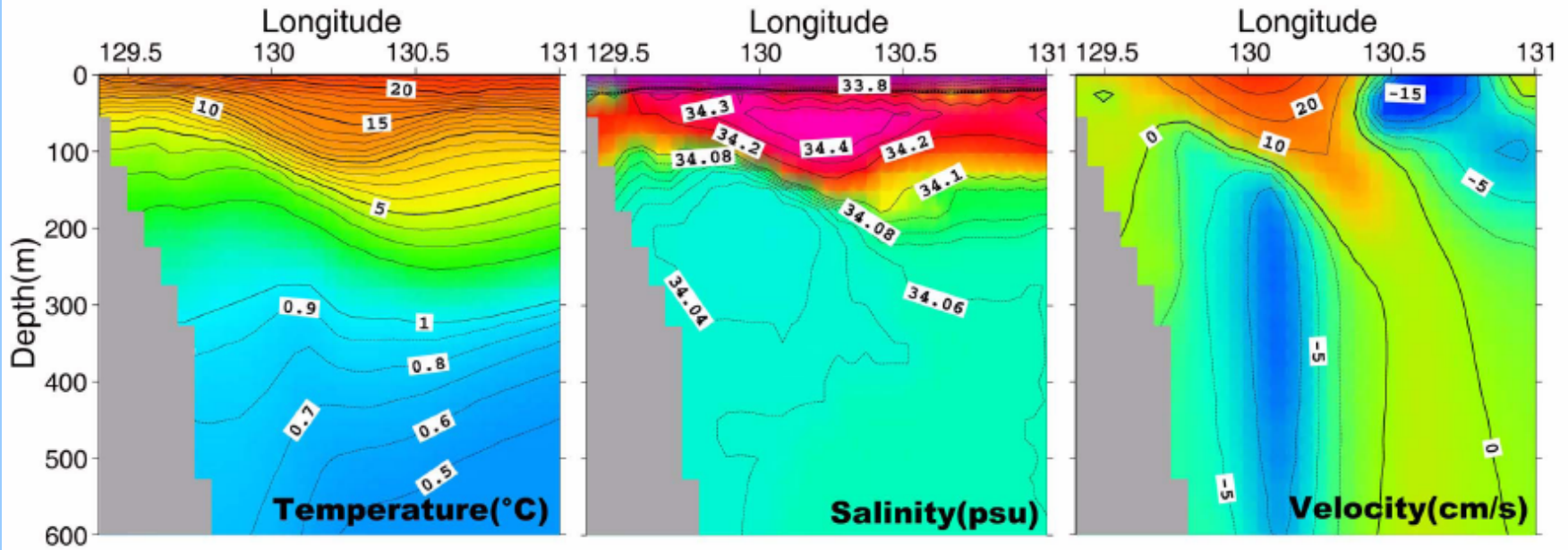


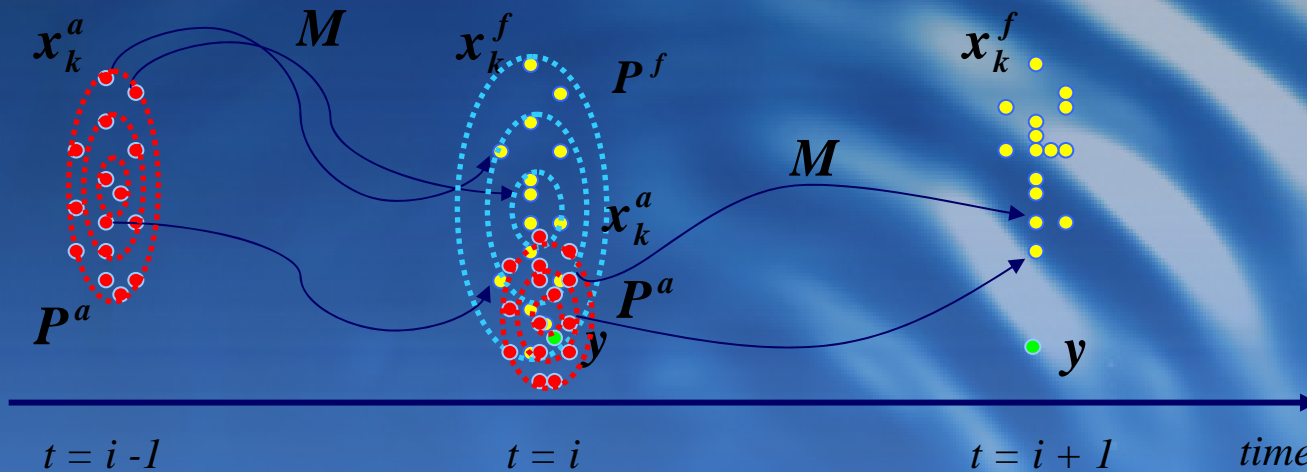
1. New scheme for SSH Anomaly assimilation
2. Reproduction of the NKCC in summer
3. Reproduction of mesoscale eddies in Ulleung Basin
4. Comparison with PIES observation at 100m
 - RMS error : 2.1°C
 - Correlation : 0.79



Spatio-temporal variation of the NKCC

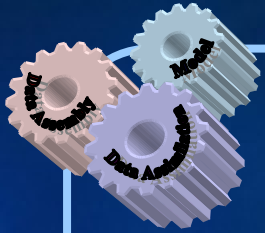
Conclusion





Implementation of EnKF

1. Direct calculation of Background Error covariance
2. Based on nonlinear ocean model
3. Localization of background error covariance
4. Inflation of background error covariance



Thank you !

